Introduction to Mobile Robotics

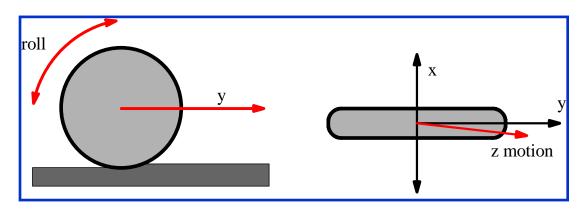
Wheeled Locomotion

Wolfram Burgard Kai Arras Maren Bennewitz Giorgio Grisetti Cyrill Stachniss

Locomotion of Wheeled Robots

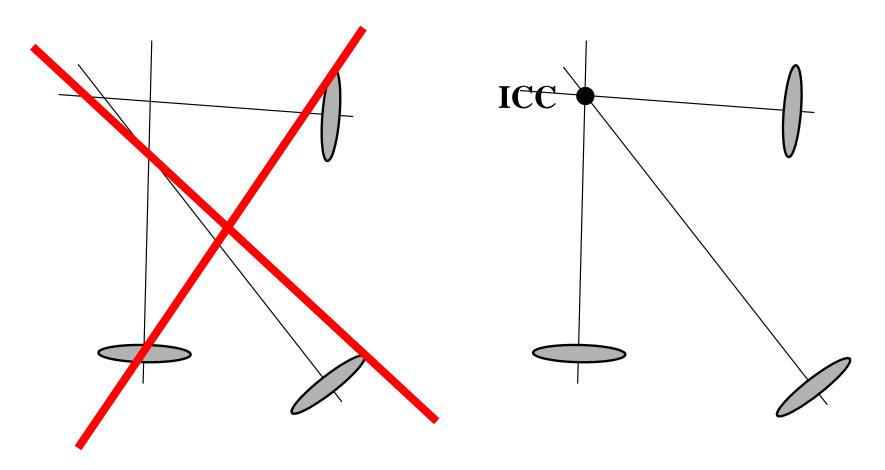
Locomotion (Oxford Dict.):

Power of motion from place to place



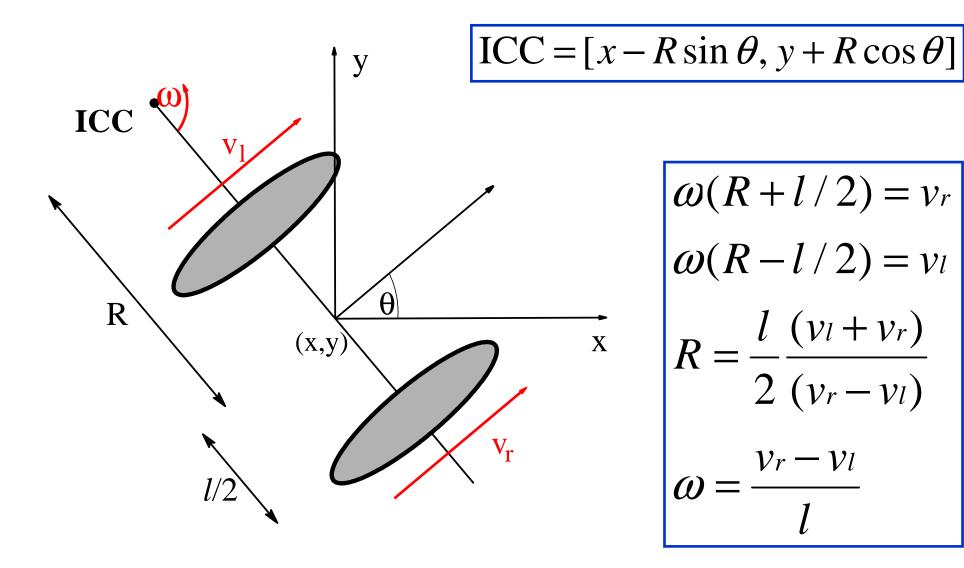
- Differential drive (AmigoBot, Pioneer 2-DX)
- Car drive (Ackerman steering)
- Synchronous drive (B21)
- Mecanum wheels, XR4000

Instantaneous Center of Curvature

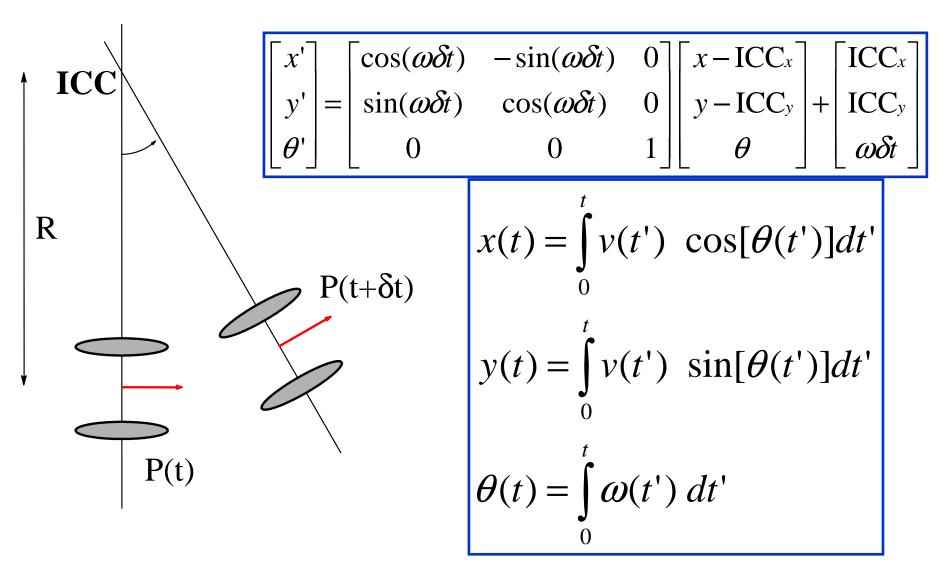


 For rolling motion to occur, each wheel has to move along its y-axis

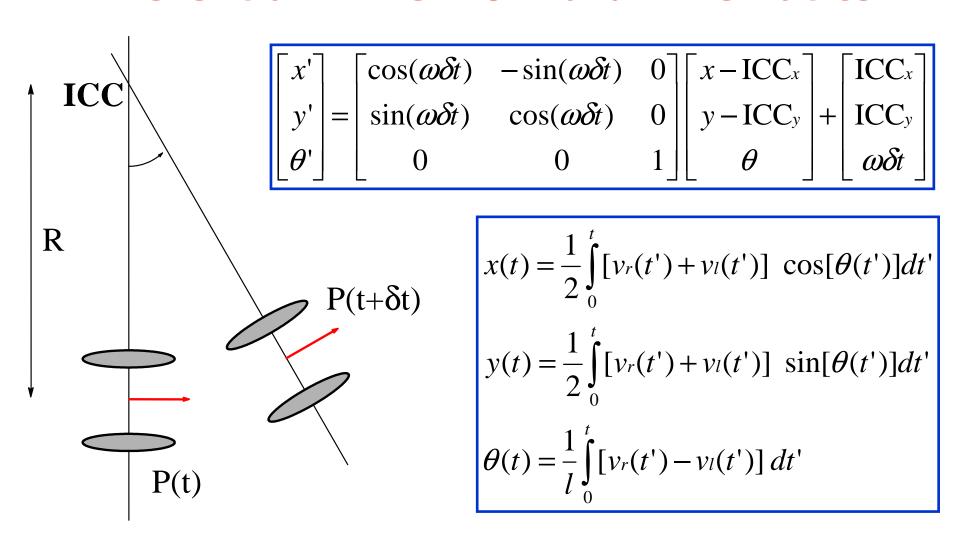
Differential Drive



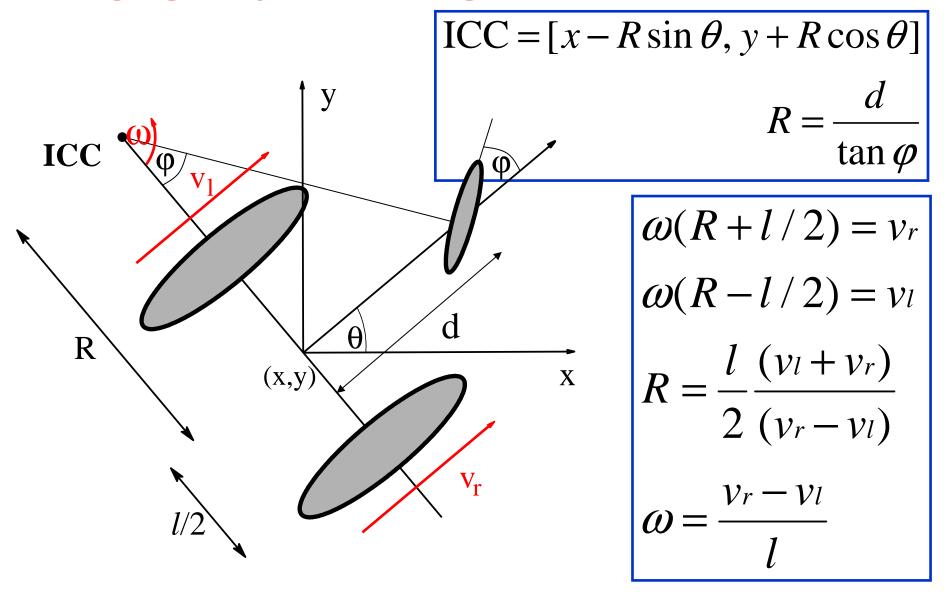
Differential Drive: Forward Kinematics



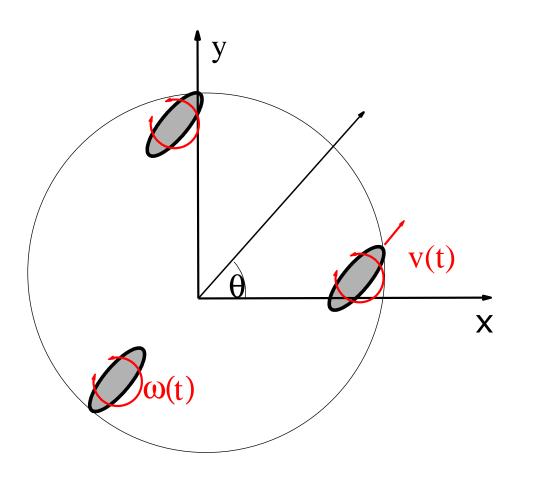
Differential Drive: Forward Kinematics



Ackermann Drive



Synchonous Drive

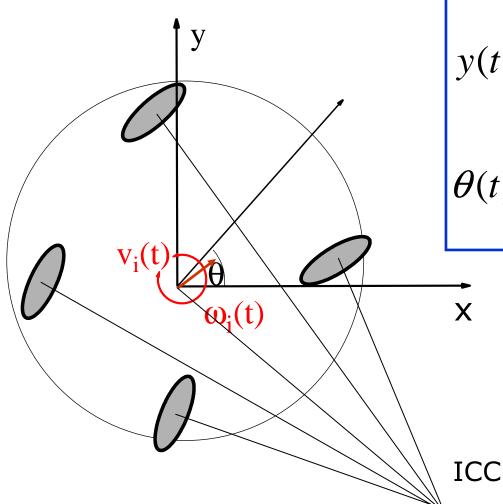


$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$

$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$

$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$

XR4000 Drive



$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$

$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$

$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$

XR4000



[courtesy by Oliver Brock & Oussama Khatib]

Mecanum Wheels



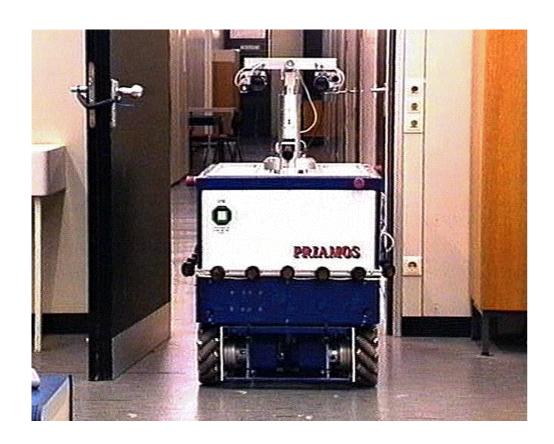
$$v_{y} = (v_{0} + v_{1} + v_{2} + v_{3})/4$$

$$v_{x} = (v_{0} - v_{1} + v_{2} - v_{3})/4$$

$$v_{\theta} = (v_{0} + v_{1} - v_{2} - v_{3})/4$$

$$v_{error} = (v_{0} - v_{1} - v_{2} + v_{3})/4$$

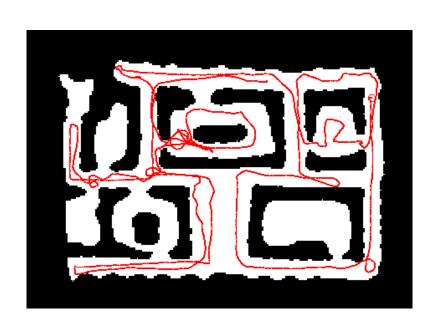
Example: Priamos (Karlsruhe)

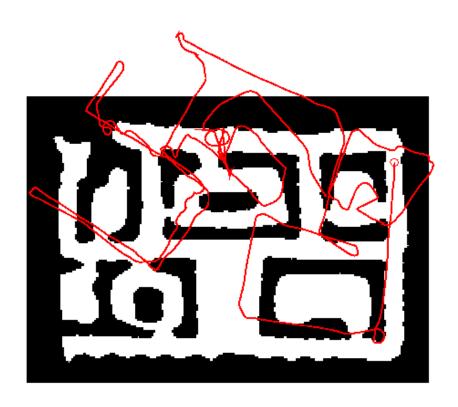


Example



Odometry





Tracked Vehicle: Urban Robot









Tracked Vehicle: OmniTread



[courtesy by Johann Borenstein]

Non-Holonomic Constraints

- Non-holonomic constraints limit the possible incremental movements within the configuration space of the robot.
- Robots with differential drive or synchro-drive move on a circular trajectory and cannot move sideways.
- XR-4000 or Mecanum-wheeled robots can move sideways (they have no non-holonomic constraints).

Holonomic vs. Non-Holonomic

- Non-holonomic constraints reduce the control space with respect to the current configuration
 - E.g., moving sideways is impossible.
- Holonomic constraints reduce the configuration space.
 - E.g., a car and a trailer (not all angles between car and trailer are possible)

Non-Holonomic Drives

- Synchro-drive
- Differential drive
- Ackerman drive

