Foundations of Artificial Intelligence

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Exercise Sheet 7 Due: Tuesday, August 02, 2011

Exercise 7.1 (Substitutions and Unification)

- (a) Compute the substitutions
 - (i) $P(x,y)\left\{\frac{x}{A}, \frac{y}{f(B)}\right\}$,
 - (ii) $P(x,y)\{\frac{x}{f(y)}\}\{\frac{y}{g(B,B)}\},\$
 - (iii) $P(x,y)\{\frac{x}{f(y)}, \frac{y}{g(B,B)}\}$, and
 - (iv) $P(x,y)\left\{\frac{z}{f(B)},\frac{x}{A}\right\}$
- (b) Apply the unification algorithm to the following set of literals: $\{R(h(x), f(h(u), y)), R(y, f(y, h(g(A))))\}$. In each step, give the values of T_k, s_k, D_k, v_k , and t_k .

Exercise 7.2 (Skolem Normal Form)

Transform the following formulae to Skolem normal form:

- (a) $F_1 = \forall x (\exists y R(x, y) \land \exists y R(y, x))$
- (b) $F_2 = \forall x \forall z (R(x, z) \Rightarrow \exists y (R(x, y) \land R(y, z)))$
- (c) $F_3 = \forall x \exists z (R(x, z) \land \neg \exists y (R(x, y) \land R(y, z)))$

Exercise 7.3 (Herbrand Expansion)

Let $F = \forall x \forall y (P(x, f(x, g(y))) \land P(h(y), f(y, y))).$

- (a) State ten minimally large terms from the Herbrand universe of F.
- (b) State five minimally large formulae from the Herbrand expansion of F.

Exercise 7.4 (Value iteration algorithm)

Consider the following grid world. The u values specify the utilities after convergence of the value iteration and r is the reward associated with a state. Assume that $\gamma = 1$ and that an agent can perform four possible actions: North, South, East und West. With probability 0.7 the agent reaches the intended state, with probability 0.2 it moves to the right of the intended direction, and with probability 0.1 to the left.

u = 8	u = 15	u = 9
u = 2	r = 2	u = 7
u = 4	u = 16	u = 11

Which is the best action an agent can execute if he is currently in the center state of the grid world? Justify your answer. Which utility does the center state have?

If you are beyond this exercise interested into getting a feeling for the behaviour of the value iteration algorithm (especially for the influence of the discount rate and the initial values of the fields), you can try out our applet at http://www.informatik.uni-freiburg.de/~burgard/vi/vi.html.

Exercise 7.5 (Policy iteration algorithm)

Let $\gamma = 0.5$ and let there be only the actions **East** and **West**. With probability 0.9 the agent reaches the intended state (or stays where he was, if the action would move him out of the grid), and with probability 0.1 he moves in the opposite direction. The reward in the three western states is -0.05 each.



Perform one step of the policy iteration algorithm. The initial policy is given by the arrows in the states. Give the linear system of equations for the first policy evaluation, a solution to the system as well as the first improved policy π_1 .

The exercise sheets may and should be handed in and be worked on in groups of three (3) students. Please fill the cover sheet¹ and attach it to your solution.

¹http://ais.informatik.uni-freiburg.de/teaching/ss11/ki/cover-sheet.pdf