Introduction to Mobile Robotics

Multi-Robot Exploration

Wolfram Burgard, Cyrill Stachniss,
Maren Bennewitz, Kai Arras
The approaches seen so far are purely passive.

Given an unknown environment, how can we control the robot(s) to efficiently learn a map?

By reasoning about control, the mapping process can be made much more effective.
Decision-Theoretic Formulation of Exploration

\[ \pi(Bel) = \arg\max_u \left[ E_z[I_{Bel}(z, u)] - \alpha \int_x r(x, u) Bel(x) \, dx \right] \]

- **reward** (expected information gain)
- **cost** (path length)
Exploration with Known Poses
Motivation

Whenever teams of mobile robots are used, the question arises, how to control them in order to optimize the performance of the whole team.

- Exploration
- Path planning
- Action planning ...
Exploration: The Problem

Given:
- Unknown environment
- Team of robots

Task:
- Coordinate the robots to efficiently learn a complete map of the environment

Complexity:
- Exponential in the number of robots
Example

Robot 1:  

Robot 2:
Levels of Coordination

- No exchange of information

- Implicit coordination (uncoordinated): Sharing a joint map [Yamauchi et.al, 98]
  - Communication of the individual maps and poses
  - Central mapping system

- Explicit coordination: Improve assignment of robots to target points
  - Communication of the individual maps and poses
  - Central mapping system
  - Central planner for target point assignment
Idea

1. Choose target locations at the frontier to the unexplored area by trading off the expected information gain and travel costs.

2. Reduce utility of target locations whenever they are expected to be covered by another robot.

3. Use on-line mapping and localization to compute the joint map.
The Coordination Algorithm (informal)

1. Determine the frontier cells.
2. Compute for each robot the cost for reaching each frontier cell.
3. Choose the robot with the optimal overall evaluation and assign the corresponding target point to it.
4. Reduce the utility of the frontier cells visible from that target point.
5. If there is one robot left go to 3.
The Coordination Algorithm

1. Determine the set of frontier cells

2. Compute for each robot $i$ the cost $V_{x,y}^i$ for reaching each frontier cell

3. Set the utility $U_{x,y}$ of all frontier cells to 1

4. While there is one robot left without a target point
   (a) Determine a robot $i$ and a frontier cell $\langle x, y \rangle$ which satisfy

   $$(i, \langle x, y \rangle) = \arg\max_{(i', \langle x', y' \rangle)} U_{x',y'} - V_{x',y'}^i$$

   (b) Reduce the utility of each target point $\langle x', y' \rangle$ in the visibility area according to

   $$U_{x',y'} \leftarrow U_{x',y'} \cdot (1 - P(|| \langle x, y \rangle - \langle x', y' \rangle ||))$$
Estimating the Visible Area

Distances measured during exploration:

Resulting probability of measuring at least distance $d$: 
Application Example

First robot:

Second robot:
Multi-Robot Exploration and Mapping of Large Environments
Resulting Map (constructed in 8 minutes!)
Further Application
Typical Trajectories in an Office Environment

Implicit coordination:

Explicit coordination:
Exploration Time

exploration time [min]

number of robots

uncoordinated
coordinated
Simulation Experiments

Implicitly coordinated:

Explicitly coordinated:
Optimizing Assignments

- The current system performs a greedy assignment of robots to target locations.

- What if we optimize the assignment?
Optimizing Assignment Algorithm

**Algorithm 2** Goal selection determining the best assignment over all permutations.

1. Determine the set of frontier cells.
2. Compute for each robot $i$ the cost $V_t^i$ for reaching each frontier cell.
3. Determine target locations $t_1, \ldots, t_n$ for the robots $i = 1, \ldots, n$ that maximizes the following evaluation function:
   \[ \sum_{i=1}^{n} U(t_i \mid t_1, \ldots, t_{i-1}, t_{i+1}, \ldots, t_n) - \beta \cdot (V_t^i)^2.\]

One approach: randomized optimization of assignments.
General Idea for Optimization

1. Start with an initial assignment
2. Select a pair of robot/target point assignments
3. If the evaluation improves if we swap the assignments

- Variants:
  - accept lower evaluations with a certain but over time decreasing probability
  - perform random restarts
Other Coordination Techniques

- Hungarian Method:
  - Optimal assignment of jobs to machines given a fixed cost matrix.
  - Similar results that the presented coordination technique.

- Market economy-guided approaches:
  - Robots trade with targets.
  - Computational load is shared between the robots
Exploration Time

![Exploration Time Graph](image-url)

The graph shows the exploration time in minutes for different numbers of robots. The lines represent uncoordinated, coordinated, randomized, and Hungarian Method strategies. As the number of robots increases, the exploration time decreases for all methods.
Summary on Exploration

- Coordination techniques that intelligently distribute the robots over the environment lead to reduced exploration time.
- Methods trade off the cost of an action and the expected utility of reaching the corresponding frontier (target location)
Open Problems

- Unknown starting locations
- Exploration under position uncertainty
- Limited communication abilities
- Efficient exchange of information
- Separation of the environment to get better target points and assignments.