

## Sheet 4

Topic: Sampling, Motion Models

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### Exercise 1: Sampling

Implement three functions in Octave which generate samples of a normal distribution  $\mathcal{N}(\mu, \sigma^2)$ . The input parameters of these functions should be the mean  $\mu$  and the variance  $\sigma^2$  of the normal distribution. As only source of randomness, use samples of a uniform distribution.

- In the first function, generate the normal distributed samples by summing up 12 uniform distributed samples, as explained in the lecture.
- In the second function, use rejection sampling.
- In the third function, use the Box-Muller transformation method. The Box-Muller method allows to generate samples from a standard normal distribution using two uniformly distributed samples  $u_1, u_2 \in [0, 1]$  via the following equation:

$$x = \cos(2\pi u_1) \sqrt{-2 \log u_2}.$$

Compare the execution times of the three functions using Octave's built-in functions `tic` and `toc`. Also, compare the execution times of your own functions to the built-in function `normrnd`.

### Exercise 2: Motion Model

A working motion model is a requirement for all Bayes Filter implementations. In the following, you will implement the simple odometry-based motion model.

- (a) Implement the odometry-based motion model in Octave. Your function should take the following three arguments

$$\mathbf{x}_t = \begin{pmatrix} x \\ y \\ \theta \end{pmatrix} \quad \mathbf{u}_t = \begin{pmatrix} \delta_{r1} \\ \delta_{r2} \\ \delta_t \end{pmatrix} \quad \boldsymbol{\alpha} = \begin{pmatrix} \alpha_1 \\ \alpha_2 \\ \alpha_3 \\ \alpha_4 \end{pmatrix},$$

where  $\mathbf{x}_t$  is the current pose of the robot,  $\mathbf{u}_t$  is the odometry reading obtained from the robot, and  $\boldsymbol{\alpha}$  are the noise parameters of the motion model. The return value of the function should be the new pose  $\mathbf{x}_{t+1}$  of the robot.

As we do not expect the odometry measurements to be perfect, you will have to take the measurement error into account when implementing your function. Use the sampling methods you implemented in Exercise 1 to draw normally distributed random numbers for the noise in the motion model.

- (b) If you evaluate your motion model over and over again with the same starting position, odometry reading, and noise values what is the result you would expect?
- (c) Evaluate your motion model 5000 times for the following values

$$\mathbf{x}_t = \begin{pmatrix} 2.0 \\ 4.0 \\ 0.0 \end{pmatrix} \quad \mathbf{u}_t = \begin{pmatrix} \frac{\pi}{2} \\ 0.0 \\ 1.0 \end{pmatrix} \quad \boldsymbol{\alpha} = \begin{pmatrix} 0.1 \\ 0.1 \\ 0.01 \\ 0.01 \end{pmatrix} .$$

Plot the resulting  $(x, y)$  positions for each of the 5000 evaluations in a single plot.