Introduction to Mobile Robotics

Wheeled Locomotion

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Locomotion of Wheeled Robots

Locomotion (Oxford Dict.): Power of motion from place to place

- Differential drive (AmigoBot, Pioneer 2-DX)
- Car drive (Ackerman steering)
- Synchronous drive (B21)
- XR4000
- Mecanum wheels



we also allow wheels to rotate around the z axis

Instantaneous Center of Curvature



 For rolling motion to occur, each wheel has to move along its y-axis

Differential Drive



Differential Drive: Forward Kinematics

ICC

$$\begin{bmatrix} x'\\ y'\\ \theta' \end{bmatrix} = \begin{bmatrix} \cos(\omega\delta t) & -\sin(\omega\delta t) & 0\\ \sin(\omega\delta t) & \cos(\omega\delta t) & 0\\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x - ICC x\\ y - ICC y\\ \theta \end{bmatrix} + \begin{bmatrix} ICC y\\ ICC y\\ \omega\delta t \end{bmatrix}$$
R

$$P(t+\delta t)$$

$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$

$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$

$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$

Differential Drive: Forward Kinematics



Ackermann Drive



Synchronous Drive



$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$
$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$
$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$

XR4000 Drive



$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$
$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$
$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$



Mecanum Wheels



$$v_{y} = (v_{0} + v_{1} + v_{2} + v_{3})/4$$

$$v_{x} = (v_{0} - v_{1} + v_{2} - v_{3})/4$$

$$v_{\theta} = (v_{0} + v_{1} - v_{2} - v_{3})/4$$

$$v_{error} = (v_{0} - v_{1} - v_{2} + v_{3})/4$$

The Kuka OmniRob Platform



Example: KUKA youBot



Tracked Vehicles









Other Robots: OmniTread



[courtesy by Johann Borenstein]

Non-Holonomic Constraints

- Non-holonomic constraints limit the possible incremental movements within the configuration space of the robot.
- Robots with differential drive or synchrodrive move on a circular trajectory and cannot move sideways.
- XR-4000 or Mecanum-wheeled robots can move sideways (they have no nonholonomic constraints).

Holonomic vs. Non-Holonomic

- Non-holonomic constraints reduce the control space with respect to the current configuration
 - E.g., moving sideways is impossible.
- Holonomic constraints reduce the configuration space.
 - E.g., a train on tracks (not all positions and orientations are possible)

Drives with Non-Holonomic Constraints

- Synchro-drive
- Differential drive
- Ackermann drive





Drives without Non-Holonomic Constraints

- XR4000 drive
- Mecanum wheels





Dead Reckoning and Odometry

- Estimating the motion based on the issued controls/wheel encoder readings
- Integrated over time





Summary

- Introduced different types of drives for wheeled robots
- Math to describe the motion of the basic drives given the speed of the wheels
- Non-holonomic constraints
- Odometry and dead reckoning