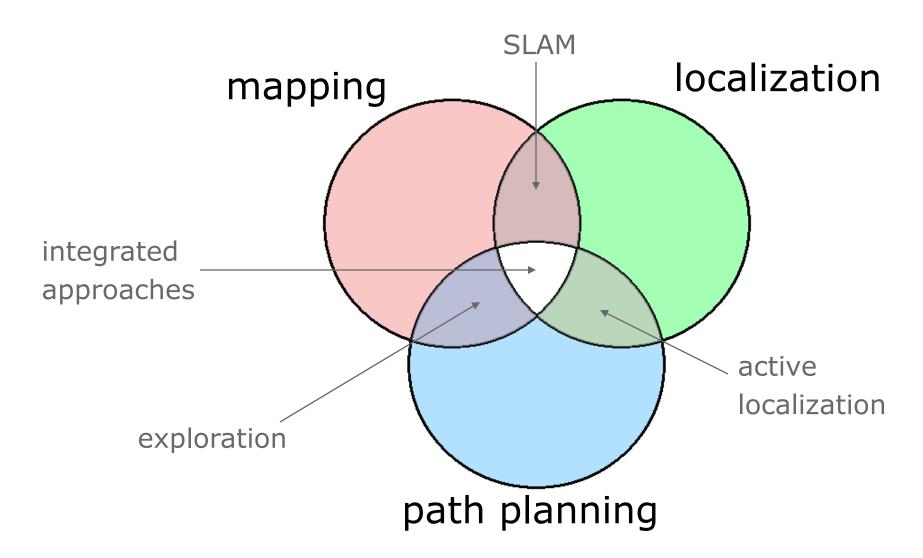
# Introduction to Mobile Robotics Information Driven Exploration

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# **Tasks of Mobile Robots**



# **Exploration and SLAM**

- SLAM is typically passive, because it consumes incoming sensor data
- Exploration actively guides the robot to cover the environment with its sensors
- Exploration in combination with SLAM: Acting under pose and map uncertainty
- Uncertainty should/needs to be taken into account when selecting an action

# Mapping with Rao-Blackwellized Particle Filter (Brief Summary)

- Each particle represents a possible trajectory of the robot
- Each particle
  - maintains its own map and
  - updates it upon "mapping with known poses"
- Each particle survives with a probability proportional to the likelihood of the observations relative to its own map

# Factorization Underlying Rao-Blackwellized Mapping

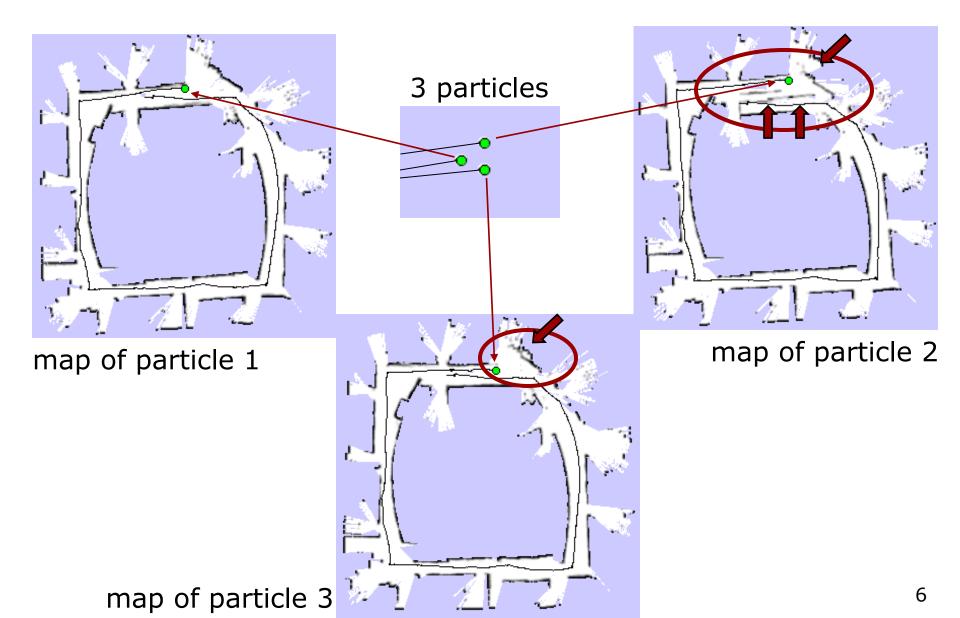
poses map observations & odometry

 $p(x, m \mid z, u)$ 

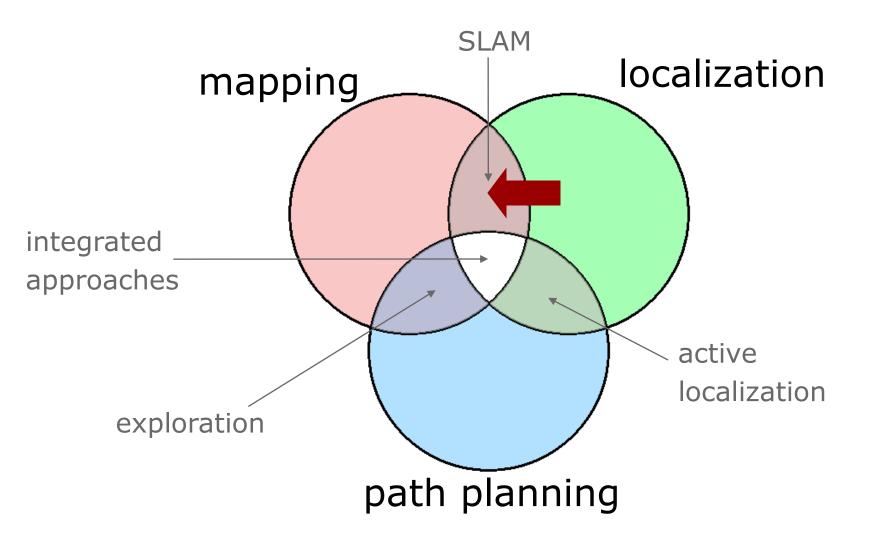
 $= p(m \mid x, z \gg) p(x \mid z, u)$ Mapping with known poses

Particle filter representing trajectory hypotheses

#### **Example: Particle Filter for Mapping**



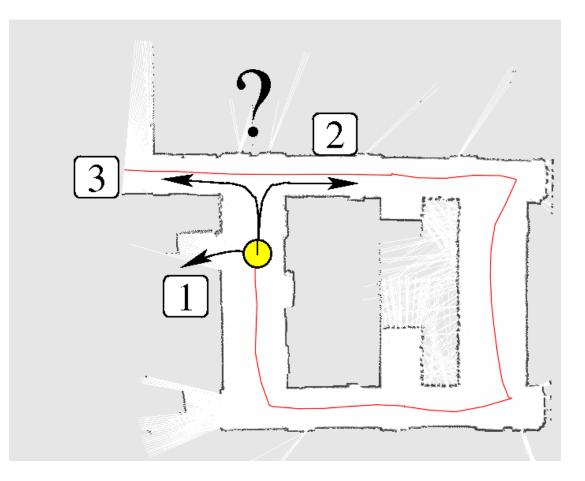
# **Combining Exploration and SLAM**



# **Exploration**

- SLAM approaches seen so far are purely passive
- By reasoning about control, the mapping process can be made much more effective
- Question: Where to move next?

#### Where to Move Next?

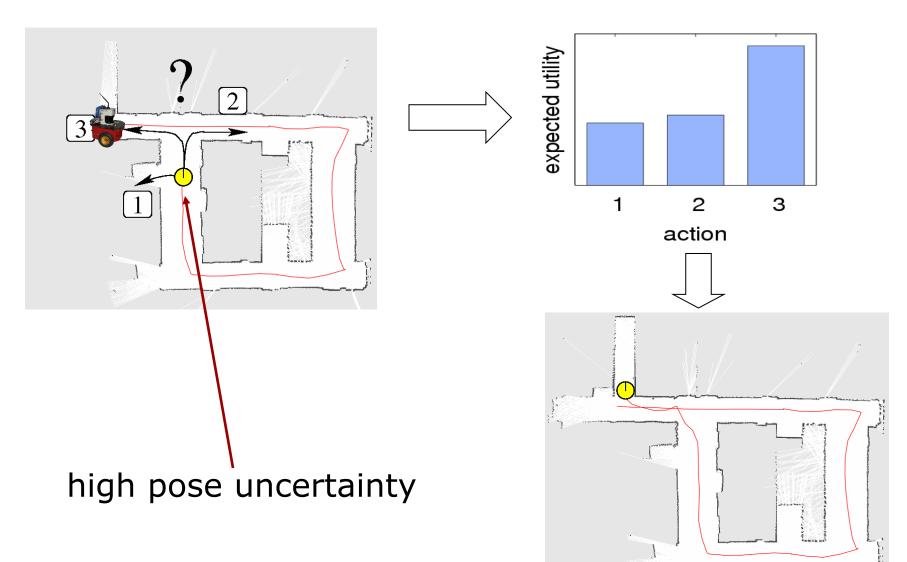


### **Decision-Theoretic Approach**

- Learn the map using a Rao-Blackwellized particle filter
- Consider a set of potential actions
- Apply an exploration approach that minimizes the overall uncertainty

#### **Utility = uncertainty reduction - cost**

#### Example



#### **The Uncertainty of a Posterior**

 Entropy is a general measure for the uncertainty of a posterior

$$H(X) = -\int_{X} p(X = x) \log p(X = x) dx$$
$$= E_X[-\log(p(X))]$$

#### Conditional Entropy

$$H(X \mid Y) = \int_{\mathcal{Y}} p(Y = y)H(X \mid Y = y) \, dy$$

# **Mutual Information**

- Expected Information Gain or Mutual Information = Expected Uncertainty Reduction
- I(X;Y) = H(X) H(X | Y) I(X;Y) = H(Y) H(Y | X)  $I(X;Y | z = c_k) = H(X | z = c_k) H(X | Y, z = c_k)$  I(X;Y | Z) = H(X | Z) H(X | Y, Z)

# **Entropy Computation**

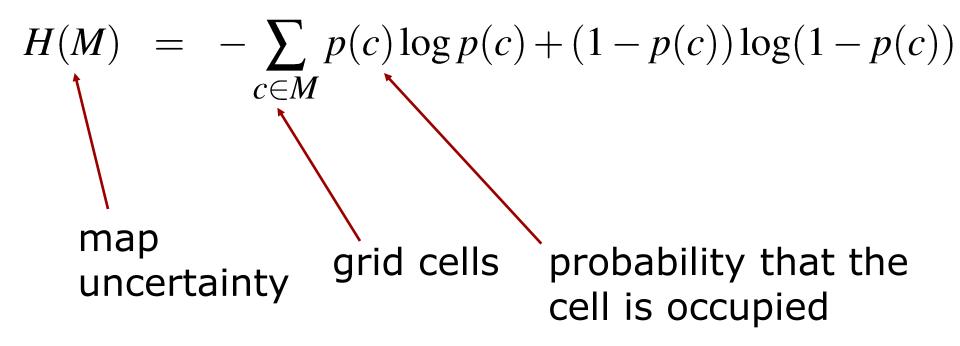
$$H(X,Y) = E_{X,Y}[-\log p(X,Y)] = E_{X,Y}[-\log (p(X) \ p(Y \mid X))] = E_{X,Y}[-\log p(X)] + E_{X,Y}[-\log p(Y \mid X)] = H(X) + \int_{x,y} -p(x,y) \log p(y \mid x) \ dx \ dx = H(X) + \int_{x,y} -p(y \mid x) p(x) \log p(y \mid x) \ dx \ dy = H(X) + \int_{x} p(x) \int_{y} -p(y \mid x) \log p(y \mid y) \ dy \ dx = H(X) + \int_{x} p(x) H(Y \mid X = x) \ dx = H(X) + H(Y \mid X)$$

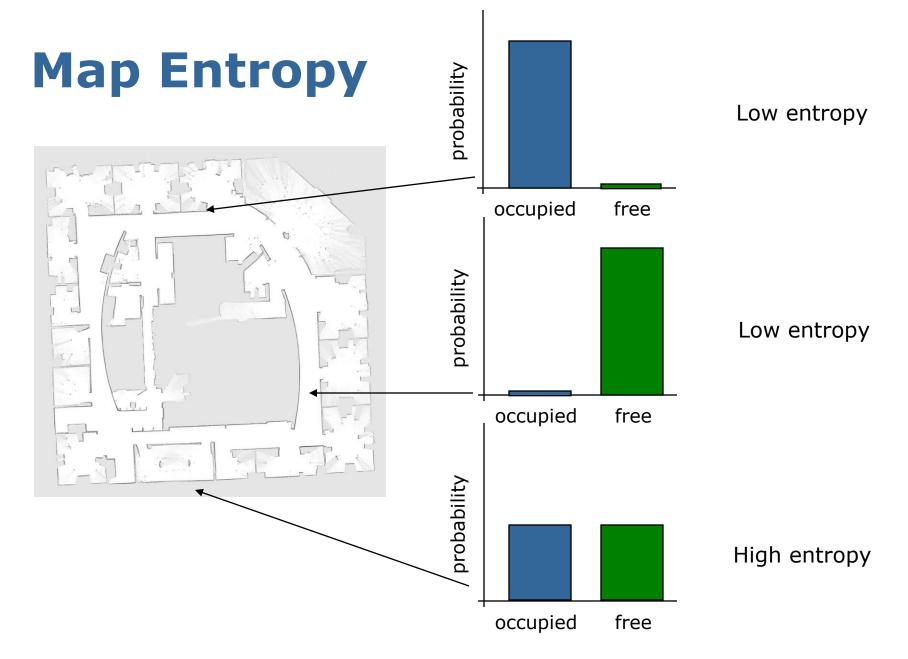
#### The Uncertainty of the Robot

The uncertainty of the RBPF:

## **Computing the Entropy of the Map Posterior**

Occupancy Grid map *m*:





The overall entropy is the sum of the individual entropy values

# **Computing the Entropy of the Trajectory Posterior**

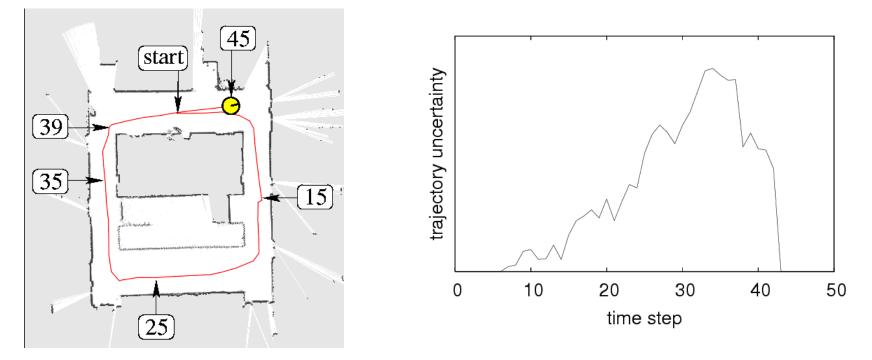
1. High-dimensional Gaussian  $H(\mathscr{G}(\mu, \Sigma)) = \log((2\pi e)^{(n/2)}|\Sigma|)$ reduced rank for sparse particle sets

2. Grid-based approximation  $H(X) \rightsquigarrow const.$ for sparse particle clouds

# **Approximation of the Trajectory Posterior Entropy**

Average pose entropy over time:

$$H(X_{1:t} \mid d) \approx \frac{1}{t} \sum_{t'=1}^{t} H(X_{t'} \mid d)$$



# **Mutual Information**

 The mutual information *I* is given by the expected reduction of entropy in the belief

action to be carried out

 $I(X,M;Z^{a}) =$  "uncertainty of the filter" – "uncertainty of the filter after carrying out action a"

#### **Integrating Over Observations**

 Computing the mutual information requires to integrate over potential observations

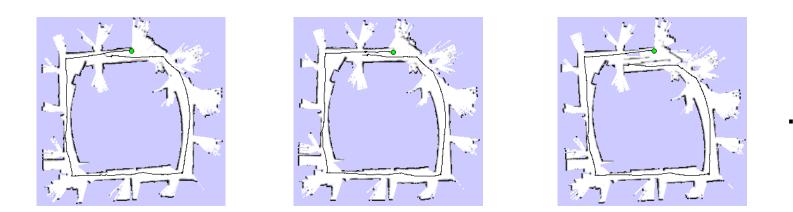
$$I(X,M;Z^{a}) = H(X,M) - H(X,M \mid Z^{a})$$

$$H(X,M \mid Z^{a}) = \int_{z} p(z \mid a) H(X,M \mid Z^{a} = z) dz$$

$$potential observation$$
sequences

# **Approximating the Integral**

 The particle filter represents a posterior about possible maps



map of particle 1 map of particle 2 map of particle 3

# **Approximating the Integral**

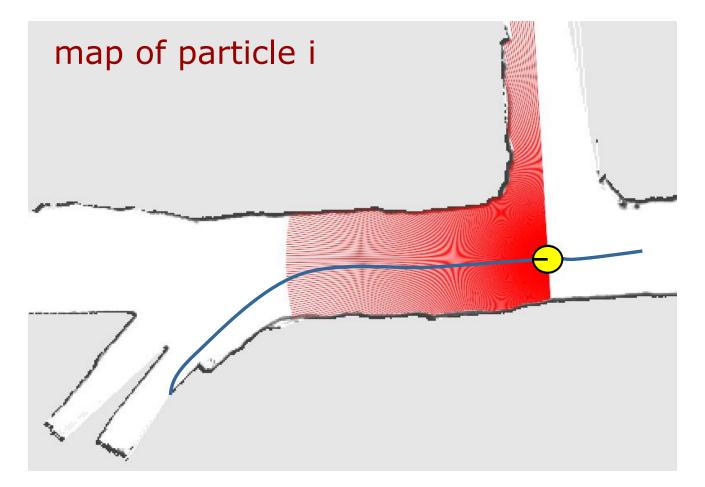
- The particle filter represents a posterior about possible maps
- Simulate laser measurements in the maps of the particles

$$H(X, M \mid Z^{a}) = \sum_{z} p(z \mid a) H(X, M \mid Z^{a} = z)$$
  
neasurement sequences  
simulated in the maps  
$$= \sum_{i} \omega^{[i]} H(X, M \mid Z^{a} = z_{sim_{a}}^{[i]})$$

m

# **Simulating Observations**

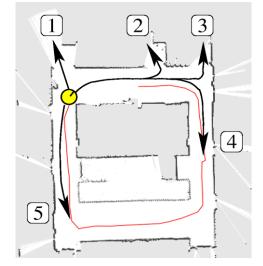
 Ray-casting in the map of each particle to generate observation sequences



# **The Utility**

- Select the action with the highest utility

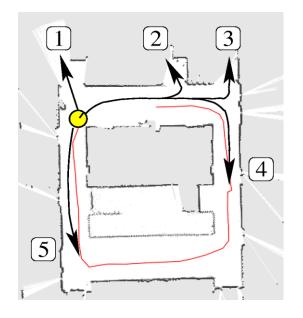
$$a^* = \operatorname{argmax}_a I(X, M; Z^a) - cost(a)$$



# **Focusing on Specific Actions**

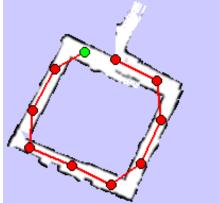
To efficiently sample actions we consider

- exploratory actions (1-3)
- Ioop closing actions (4) and
- place revisiting actions (5)

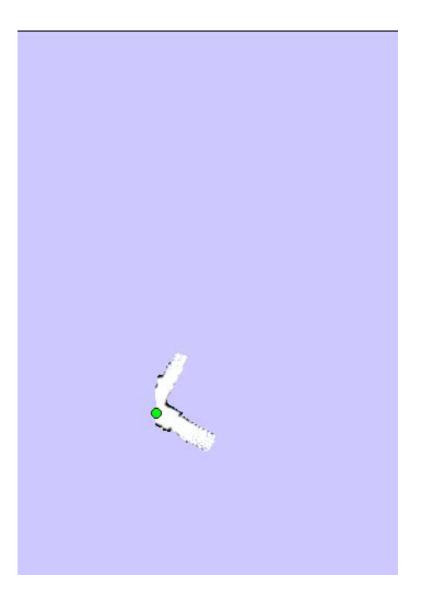


# **Dual Representation for Loop Detection**

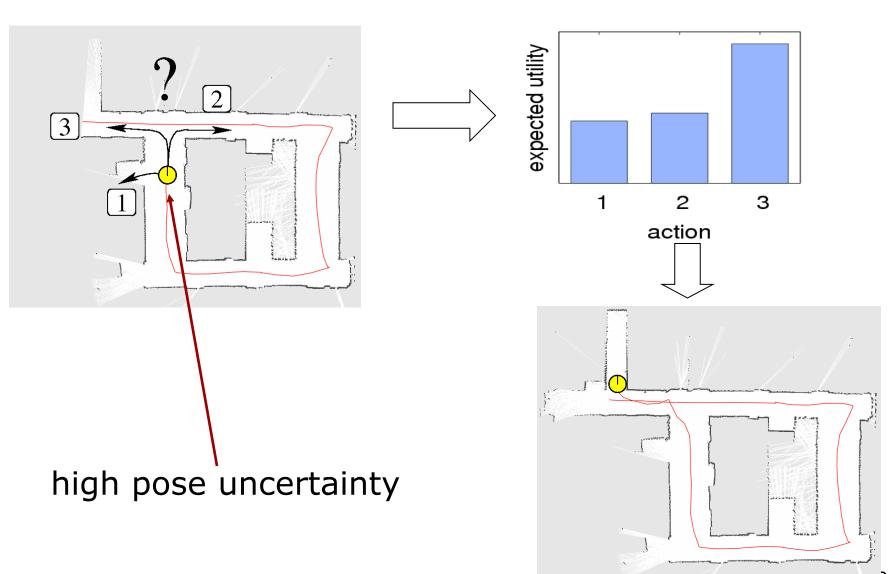
- Trajectory graph ("topological map") stores the path traversed by the robot
- Occupancy grid map represents the space covered by the sensors
- Loops correspond to long paths in the trajectory graph and short paths in the grid map



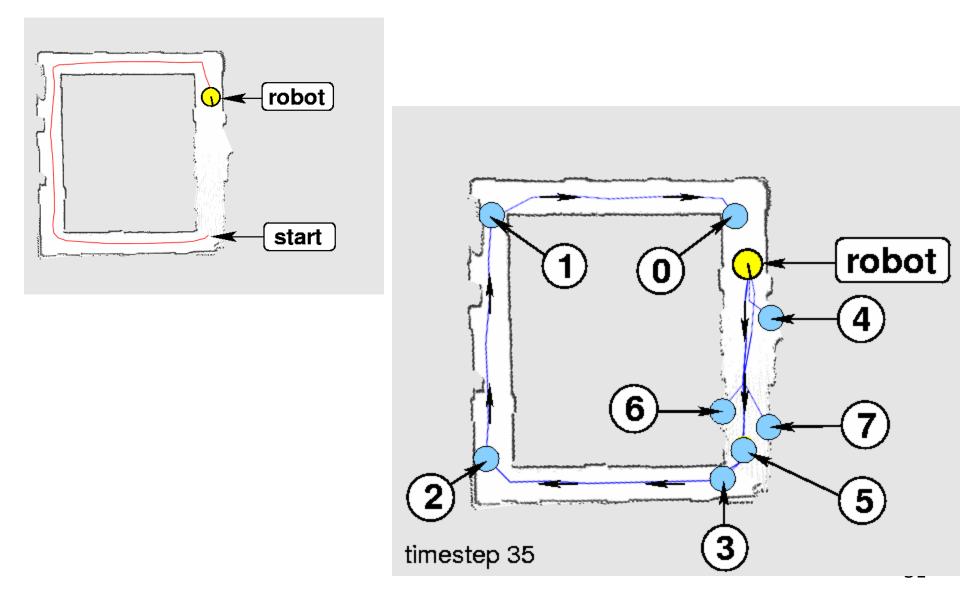
# **Example: Trajectory Graph**



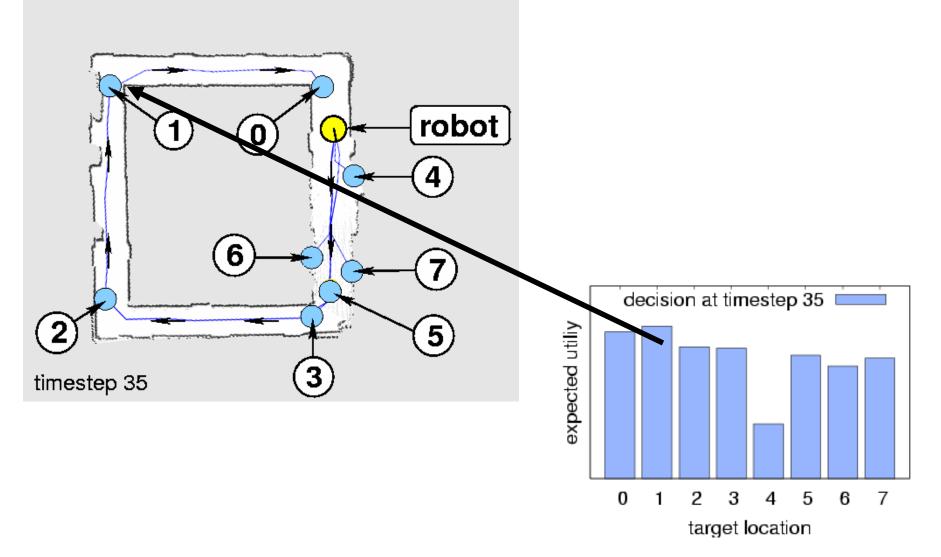
# **Application Example**



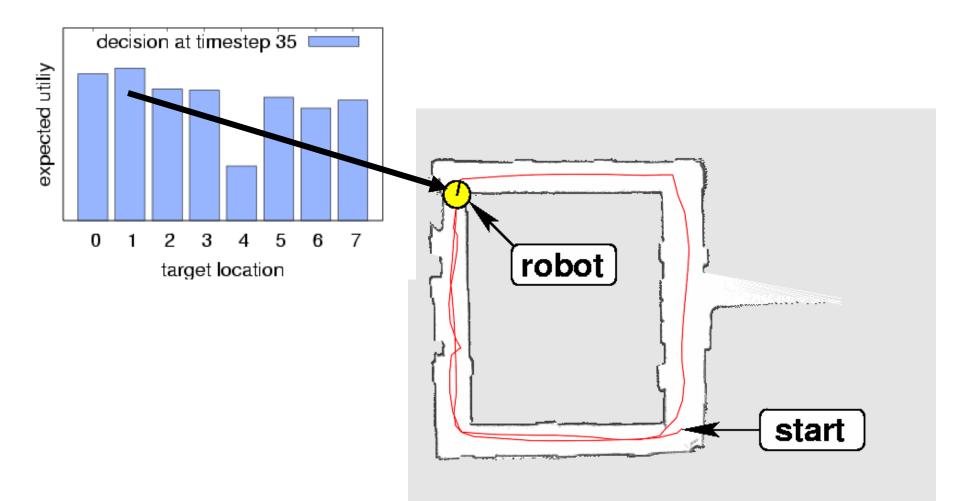
#### **Example: Possible Targets**



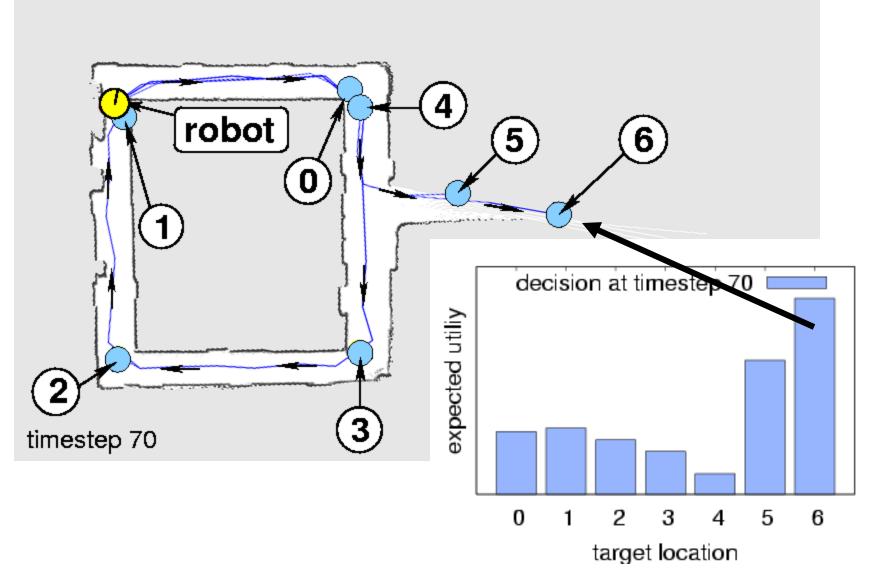
#### **Example: Evaluate Targets**



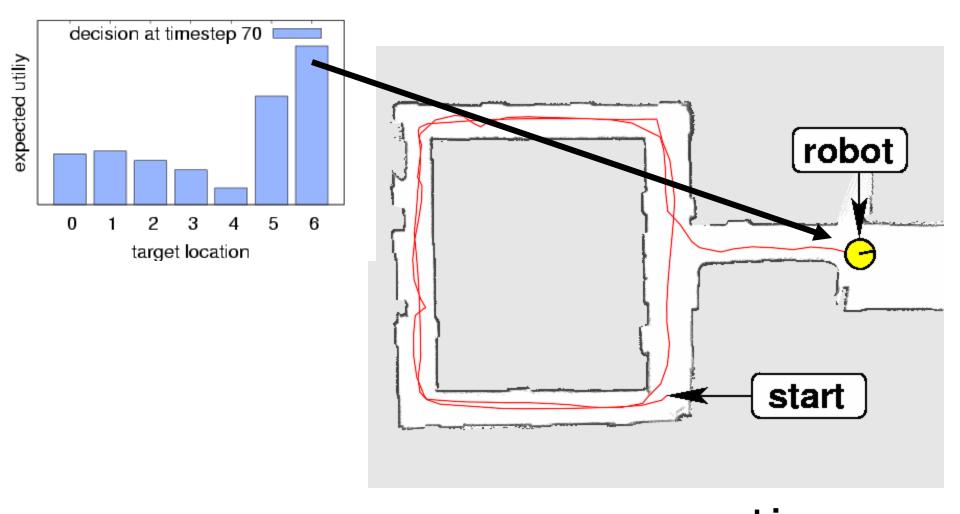
# **Example: Move Robot to Target**



#### **Example: Evaluate Targets**

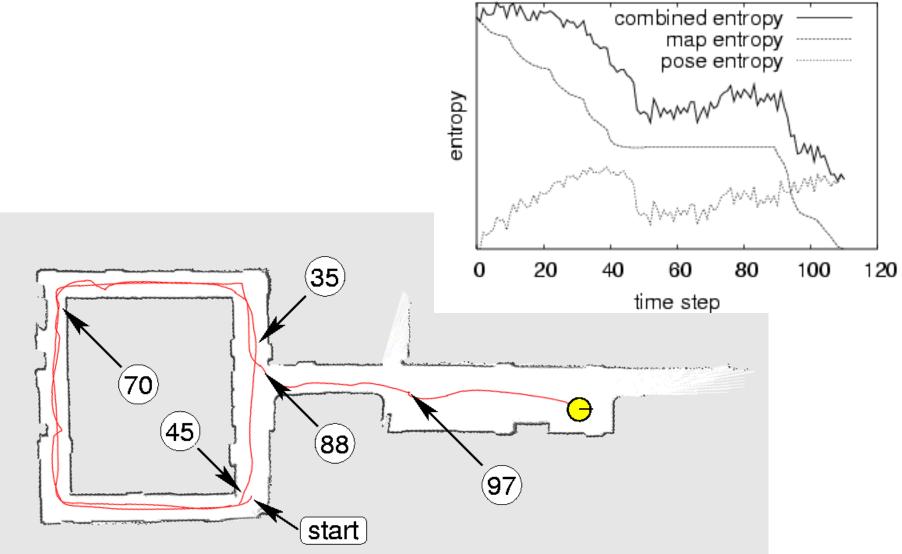


#### **Example: Move Robot**



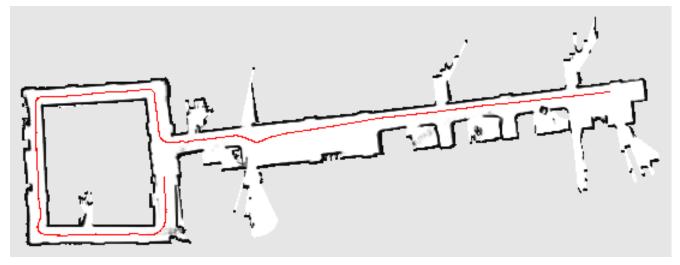
... continue .35

# **Example: Entropy Evolution**



# Comparison

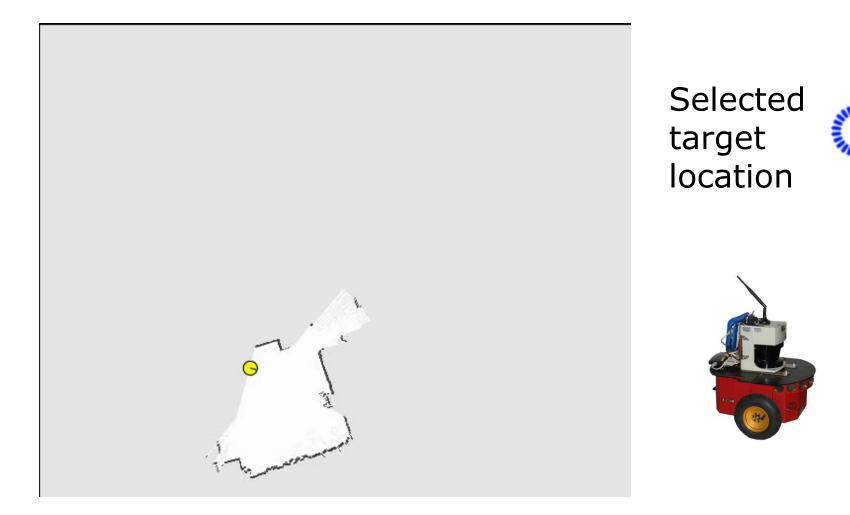
#### Map uncertainty only:



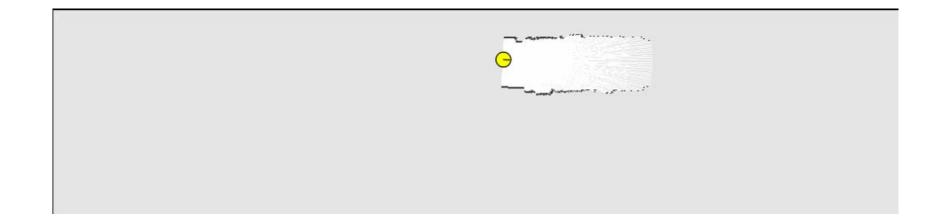
#### After loop closing action:



# **Real Exploration Example**



# **Corridor Exploration**



- The decision-theoretic approach leads to intuitive behaviors: "re-localize before getting lost"
- Some animals show a similar behavior (dogs marooned in the tundra of north Russia)

# Summary

- A decision-theoretic approach to exploration in the context of RBPF-SLAM
- The approach utilizes the factorization of the Rao-Blackwellization to efficiently calculate the expected information gain
- Reasons about measurements obtained along the path of the robot
- Considers a reduced action set consisting of exploration, loop-closing, and placerevisiting actions