

Sheet 9

Topic: Mapping with Known Poses

Due date: 24.06.2016

Exercise 1: Counting Model

A robot applies the so-called simple counting approach to build a grid map of a 1D environment consisting of the cells c_0, \dots, c_3 . While standing in cell c_0 , the robot integrates four measurements z_{t_0}, \dots, z_{t_3} . After integrating these measurements, the resulting belief of the robot with regards to the occupancy of the four cells is $b_0 = 0$, $b_1 = \frac{1}{4}$, $b_2 = \frac{2}{3}$, $b_3 = 1$. Given that the first three measurements are $z_{t_0} = 1$, $z_{t_1} = 2$, $z_{t_2} = 3$, compute the value of the last measurement z_{t_3} .

Exercise 2: Occupancy Mapping

A robot has to build an occupancy grid map (cells c_0, \dots, c_n) of a simple one-dimensional environment using a sequence of measurements from a range sensor.



Assume a very simple sensor model: every grid cell with a distance (based on its coordinate) smaller than the measured distance is assumed to be occupied with $p = 0.3$. Every cell behind the measured distance is occupied with $p = 0.6$. Every cell located more than $20cm$ behind the measured distance should not be updated. Calculate the resulting occupancy grid map using the inverse sensor model (see mapping lecture PDF, slide 10).

Use Octave. Use one array $m=0.5*\text{ones}(1,21)$ for the belief values, and one array $c=[0:10:200]$ for the cell coordinates. Use `plot(c,m)` to visualize the belief.

grid resolution	10cm
map length (1d only!)	2m
robot's position	c_0
orientation (of the sensor)	heading to c_n (see figure)
measurements (in cm)	101, 82, 91, 112, 99, 151, 96, 85, 99, 105
prior	0.5

Exercise 3: Occupancy Mapping

Proove that in the occupancy grid mapping framework the occupancy value of a grid cell $P(m_j|x_{1:t}; z_{1:t})$ is independent of the order in which the measurements are integrated.