

## Sheet 9

Topic: Mapping with Known Poses

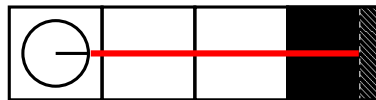
Due date: 24.06.2016

### Exercise 1: Counting Model

A robot applies the so-called simple counting approach to build a grid map of a 1D environment consisting of the cells  $c_0, \dots, c_3$ . While standing in cell  $c_0$ , the robot integrates four measurements  $z_{t_0}, \dots, z_{t_3}$ . After integrating these measurements, the resulting belief of the robot with regards to the occupancy of the four cells is  $b_0 = 0$ ,  $b_1 = \frac{1}{4}$ ,  $b_2 = \frac{2}{3}$ ,  $b_3 = 1$ . Given that the first three measurements are  $z_{t_0} = 1$ ,  $z_{t_1} = 2$ ,  $z_{t_2} = 3$ , compute the value of the last measurement  $z_{t_3}$ .

### Exercise 2: Occupancy Mapping

A robot has to build an occupancy grid map (cells  $c_0, \dots, c_n$ ) of a simple one-dimensional environment using a sequence of measurements from a range sensor.



Assume a very simple sensor model: every grid cell with a distance (based on its coordinate) smaller than the measured distance is assumed to be occupied with  $p = 0.3$ . Every cell behind the measured distance is occupied with  $p = 0.6$ . Every cell located more than  $20cm$  behind the measured distance should not be updated. Calculate the resulting occupancy grid map using the inverse sensor model (see mapping lecture PDF, slide 10).

Use Python. Use one array `m=0.5*numpy.ones(21)` for the belief values, and one array which spans from 0 to 200 (both endpoints included) with increments of 10 for the cell coordinates. You can use the following custom range function to include endpoints using Python's in built range function.

```
range_cl = lambda start, end: range(start, end+1,10)  
c = range_cl(0,200)
```

Use `matplotlib.pyplot.plot(c,m)` to visualize the belief.

grid resolution	$10cm$
map length (1d only!)	$2m$
robot's position	$c_0$
orientation (of the sensor)	heading to $c_n$ (see figure)
measurements (in cm)	101, 82, 91, 112, 99, 151, 96, 85, 99, 105
prior	0.5

### Exercise 3: Occupancy Mapping

Prove that in the occupancy grid mapping framework the occupancy value of a grid cell  $P(m_j|x_{1:t}; z_{1:t})$  is independent of the order in which the measurements are integrated.