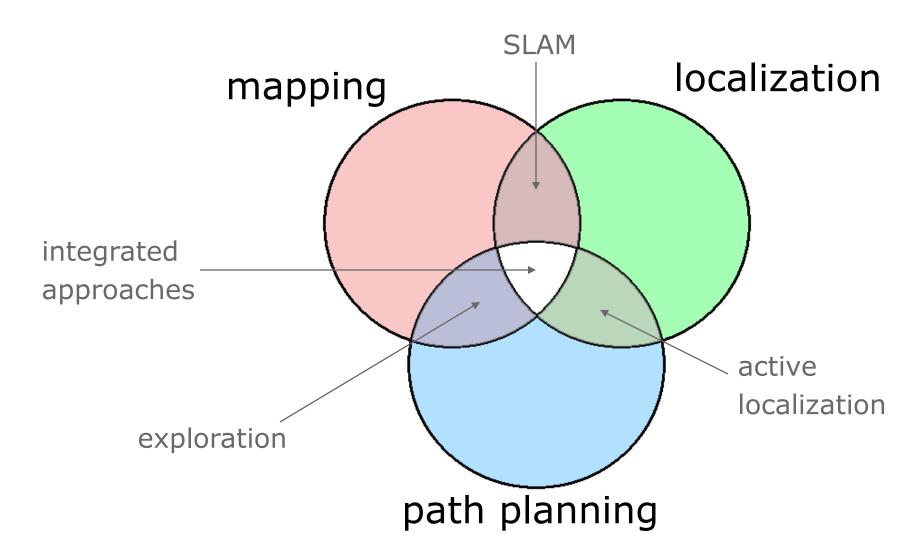
Introduction to Mobile Robotics Information Driven Exploration

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Tasks of Mobile Robots



Exploration and SLAM

- SLAM is typically passive, because it consumes incoming sensor data
- Exploration actively guides the robot to cover the environment with its sensors
- Exploration in combination with SLAM: Acting under pose and map uncertainty
- Uncertainty should/needs to be taken into account when selecting an action

Mapping with Rao-Blackwellized Particle Filter (Brief Summary)

- Each particle represents a possible trajectory of the robot
- Each particle
 - maintains its own map and
 - updates it upon "mapping with known poses"
- Each particle survives with a probability proportional to the likelihood of the observations relative to its own map

Factorization Underlying Rao-Blackwellized Mapping

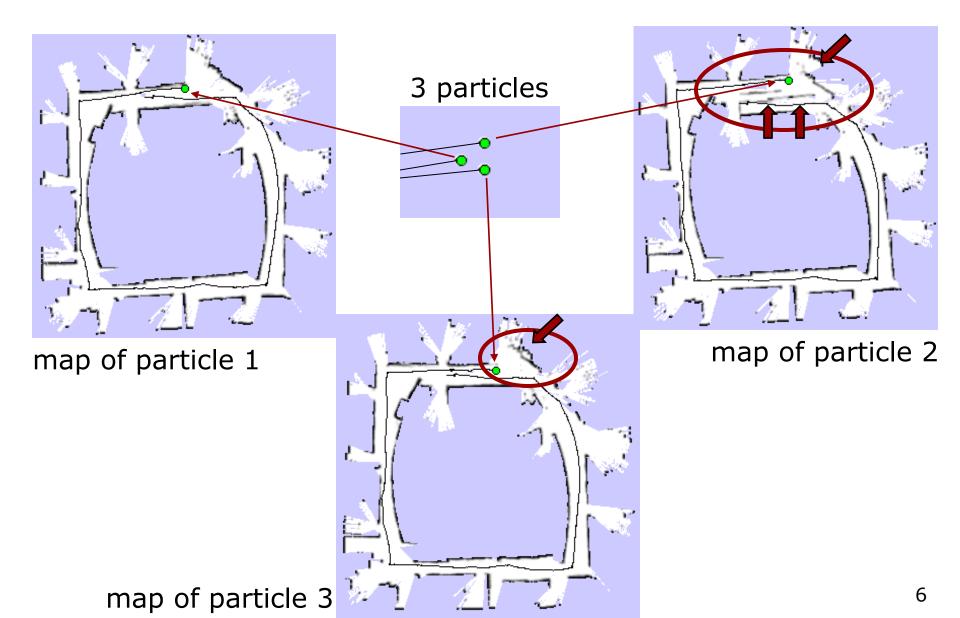
poses map observations & odometry

 $p(x, m \mid z, u)$

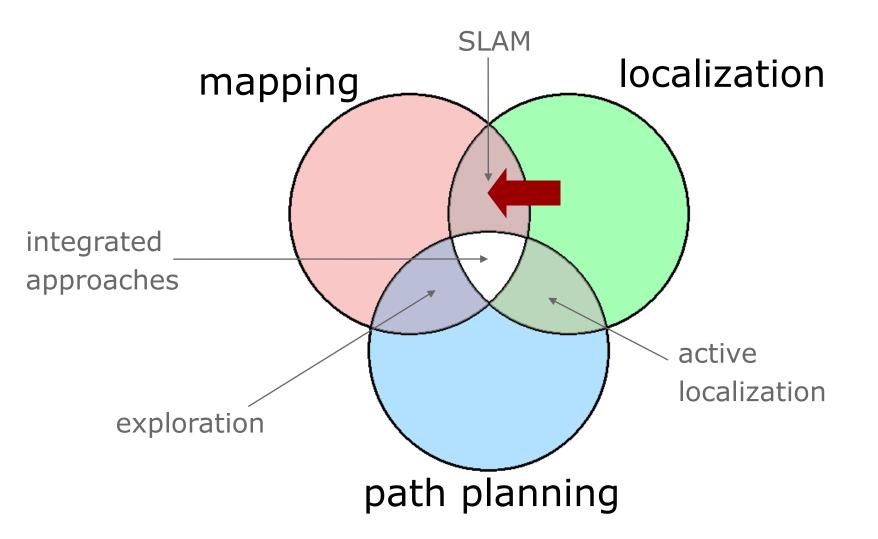
 $= p(m \mid x, z \gg) p(x \mid z, u)$ Mapping with known poses

Particle filter representing trajectory hypotheses

Example: Particle Filter for Mapping



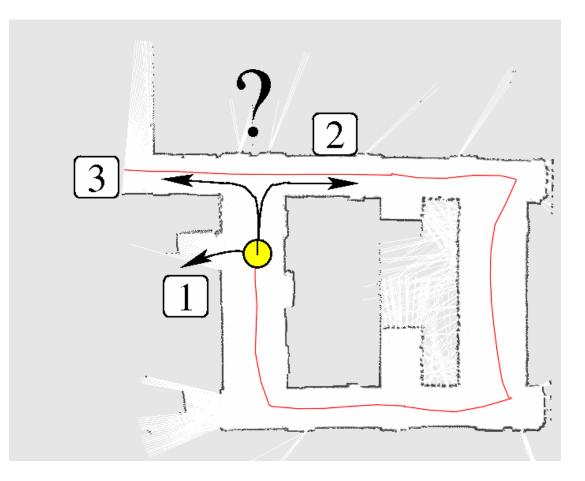
Combining Exploration and SLAM



Exploration

- SLAM approaches seen so far are purely passive
- By reasoning about control, the mapping process can be made much more effective
- Question: Where to move next?

Where to Move Next?

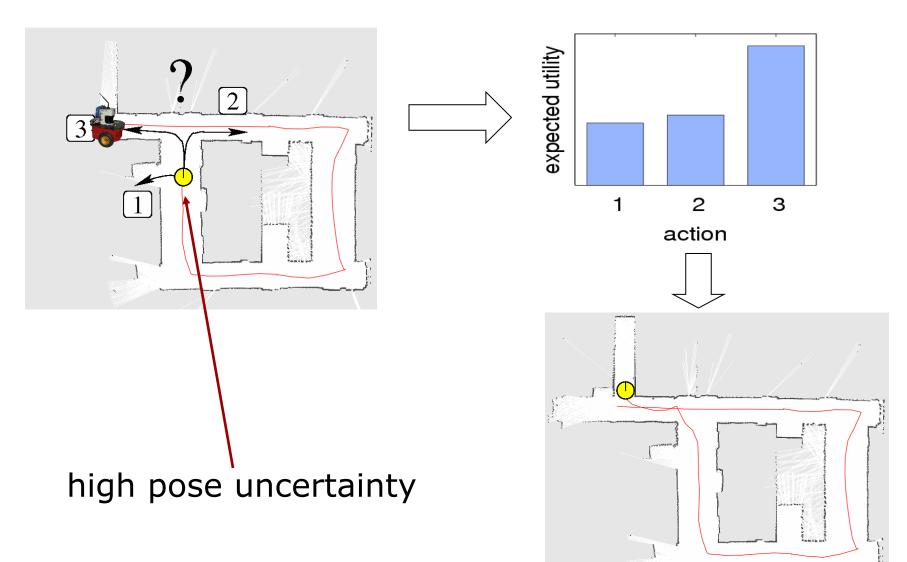


Decision-Theoretic Approach

- Learn the map using a Rao-Blackwellized particle filter
- Consider a set of potential actions
- Apply an exploration approach that minimizes the overall uncertainty

Utility = uncertainty reduction - cost

Example



The Uncertainty of a Posterior

 Entropy is a general measure for the uncertainty of a posterior

$$H(X) = -\int_{X} p(X = x) \log p(X = x) dx$$
$$= E_X[-\log(p(X))]$$

Conditional Entropy

$$H(X \mid Y) = \int_{\mathcal{Y}} p(Y = y)H(X \mid Y = y) \, dy$$

Mutual Information

- Expected Information Gain or Mutual Information = Expected Uncertainty Reduction
- I(X;Y) = H(X) H(X | Y) I(X;Y) = H(Y) H(Y | X) $I(X;Y | z = c_k) = H(X | z = c_k) H(X | Y, z = c_k)$ I(X;Y | Z) = H(X | Z) H(X | Y, Z)

Entropy Computation

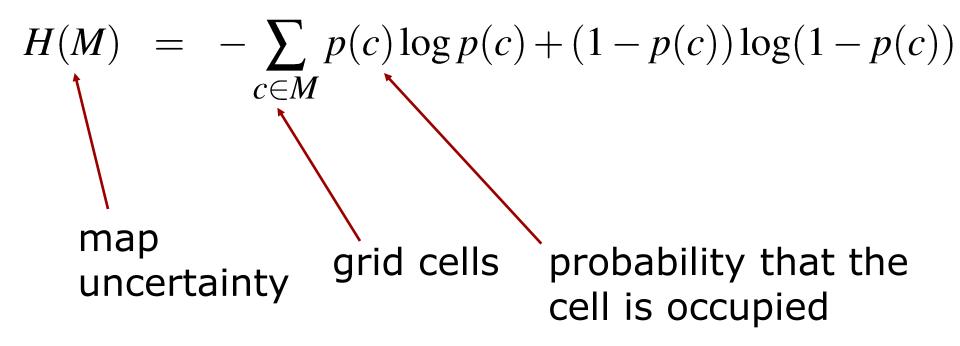
$$H(X,Y) = E_{X,Y}[-\log p(X,Y)] = E_{X,Y}[-\log (p(X) \ p(Y \mid X))] = E_{X,Y}[-\log p(X)] + E_{X,Y}[-\log p(Y \mid X)] = H(X) + \int_{x,y} -p(x,y) \log p(y \mid x) \ dx \ dx = H(X) + \int_{x,y} -p(y \mid x) p(x) \log p(y \mid x) \ dx \ dy = H(X) + \int_{x} p(x) \int_{y} -p(y \mid x) \log p(y \mid y) \ dy \ dx = H(X) + \int_{x} p(x) H(Y \mid X = x) \ dx = H(X) + H(Y \mid X)$$

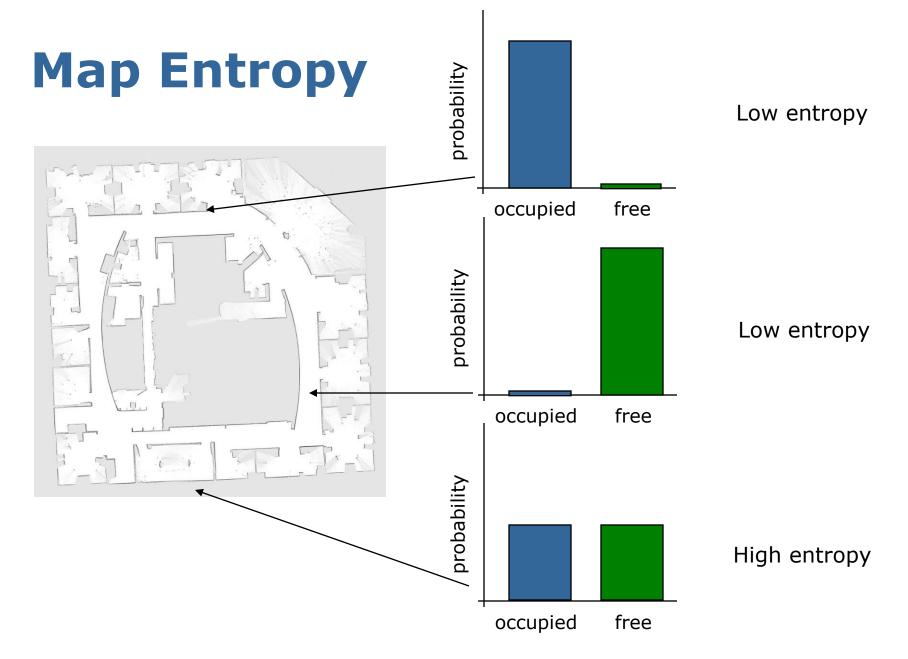
The Uncertainty of the Robot

• The uncertainty of the RBPF:

Computing the Entropy of the Map Posterior

Occupancy Grid map *m*:





The overall entropy is the sum of the individual entropy values

Computing the Entropy of the Trajectory Posterior

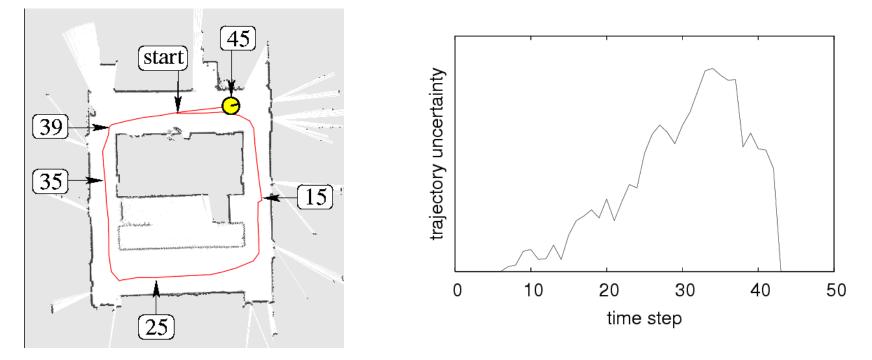
1. High-dimensional Gaussian $H(\mathscr{G}(\mu, \Sigma)) = \log((2\pi e)^{(n/2)}|\Sigma|)$ reduced rank for sparse particle sets

2. Grid-based approximation $H(X) \rightsquigarrow const.$ for sparse particle clouds

Approximation of the Trajectory Posterior Entropy

Average pose entropy over time:

$$H(X_{1:t} \mid d) \approx \frac{1}{t} \sum_{t'=1}^{t} H(X_{t'} \mid d)$$



Mutual Information

 The mutual information *I* is given by the expected reduction of entropy in the belief

action to be carried out

 $I(X,M;Z^{a}) =$ "uncertainty of the filter" – "uncertainty of the filter after carrying out action a"

Integrating Over Observations

 Computing the mutual information requires to integrate over potential observations

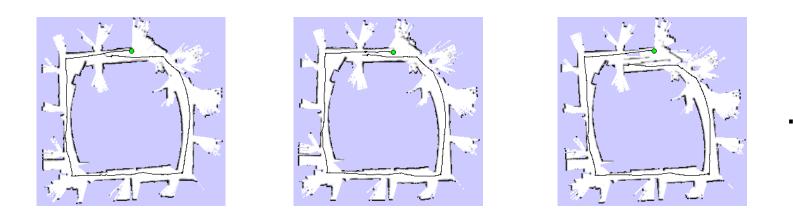
$$I(X,M;Z^{a}) = H(X,M) - H(X,M \mid Z^{a})$$

$$H(X,M \mid Z^{a}) = \int_{z} p(z \mid a) H(X,M \mid Z^{a} = z) dz$$

$$potential observation$$
sequences

Approximating the Integral

 The particle filter represents a posterior about possible maps



map of particle 1 map of particle 2 map of particle 3

Approximating the Integral

- The particle filter represents a posterior about possible maps
- Simulate laser measurements in the maps of the particles

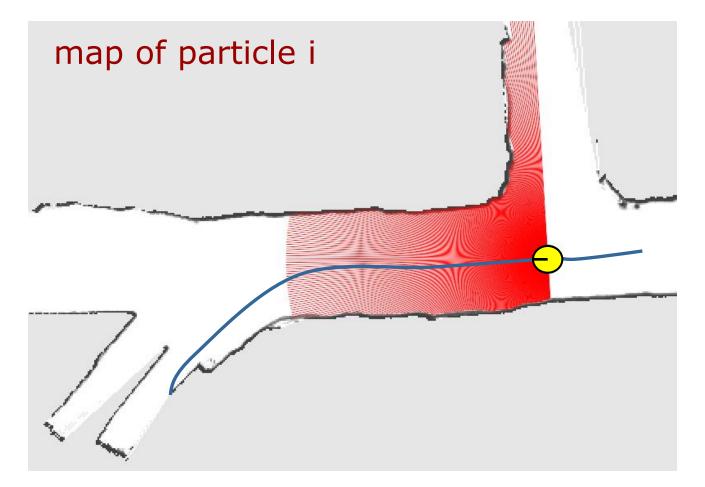
$$H(X, M \mid Z^{a}) = \sum_{z} p(z \mid a) H(X, M \mid Z^{a} = z)$$

neasurement sequences
simulated in the maps
$$= \sum_{i} \omega^{[i]} H(X, M \mid Z^{a} = z_{sim_{a}}^{[i]})$$

m

Simulating Observations

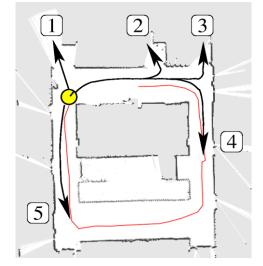
 Ray-casting in the map of each particle to generate observation sequences



The Utility

- Select the action with the highest utility

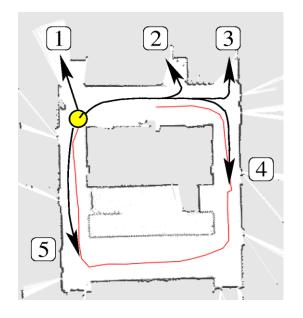
$$a^* = \operatorname{argmax}_a I(X, M; Z^a) - cost(a)$$



Focusing on Specific Actions

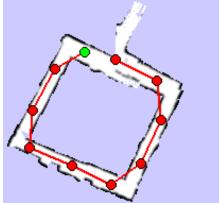
To efficiently sample actions we consider

- exploratory actions (1-3)
- Ioop closing actions (4) and
- place revisiting actions (5)

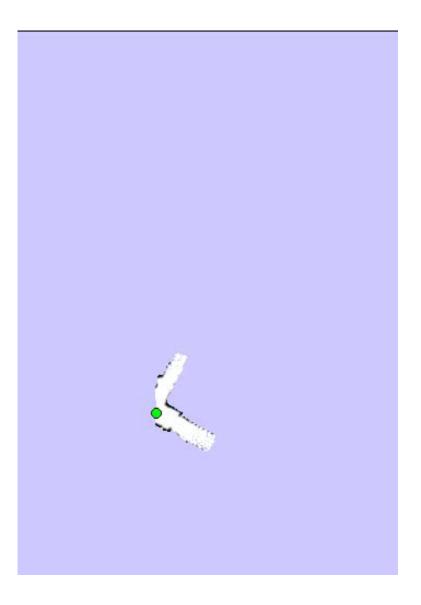


Dual Representation for Loop Detection

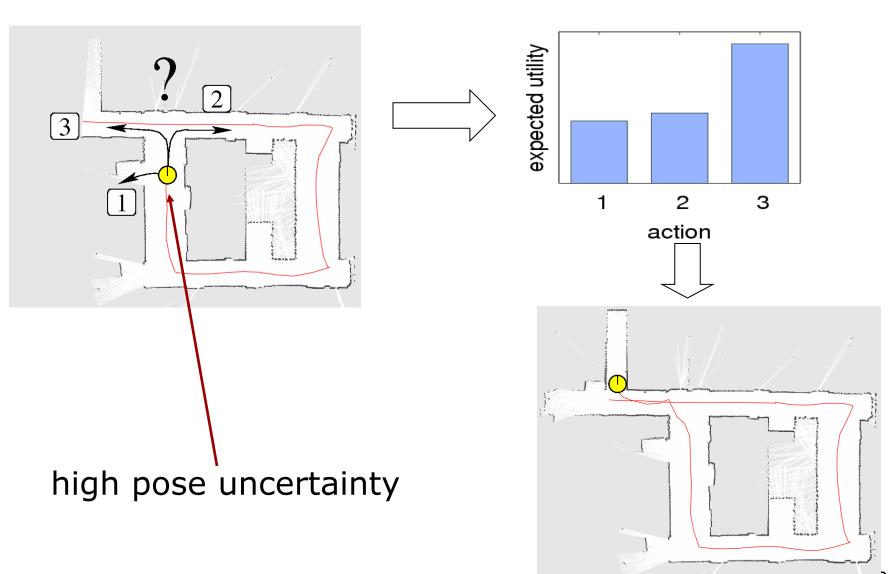
- Trajectory graph ("topological map") stores the path traversed by the robot
- Occupancy grid map represents the space covered by the sensors
- Loops correspond to long paths in the trajectory graph and short paths in the grid map



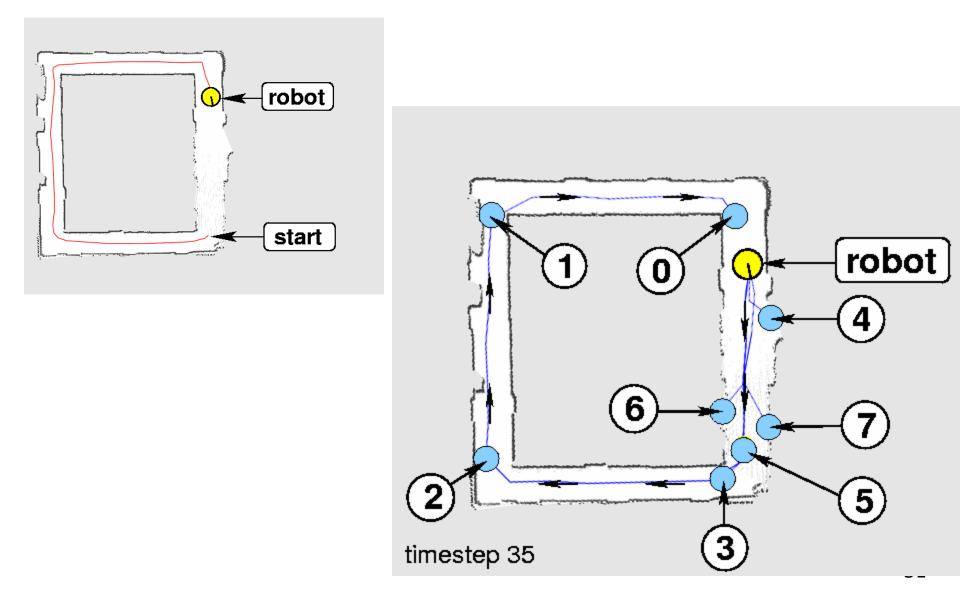
Example: Trajectory Graph



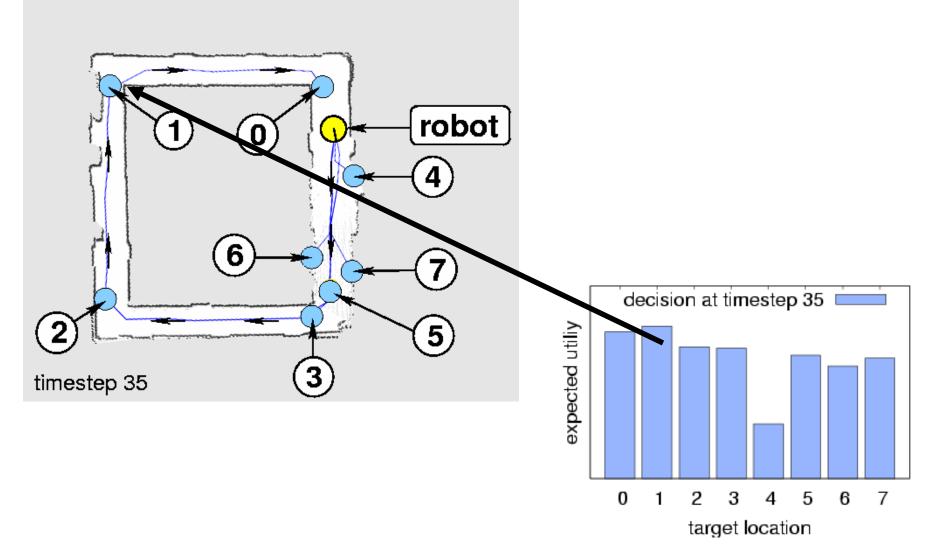
Application Example



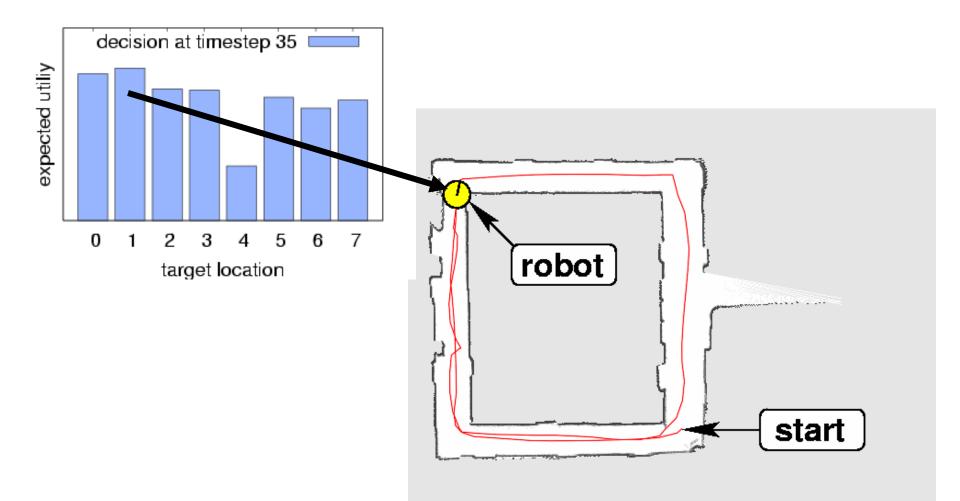
Example: Possible Targets



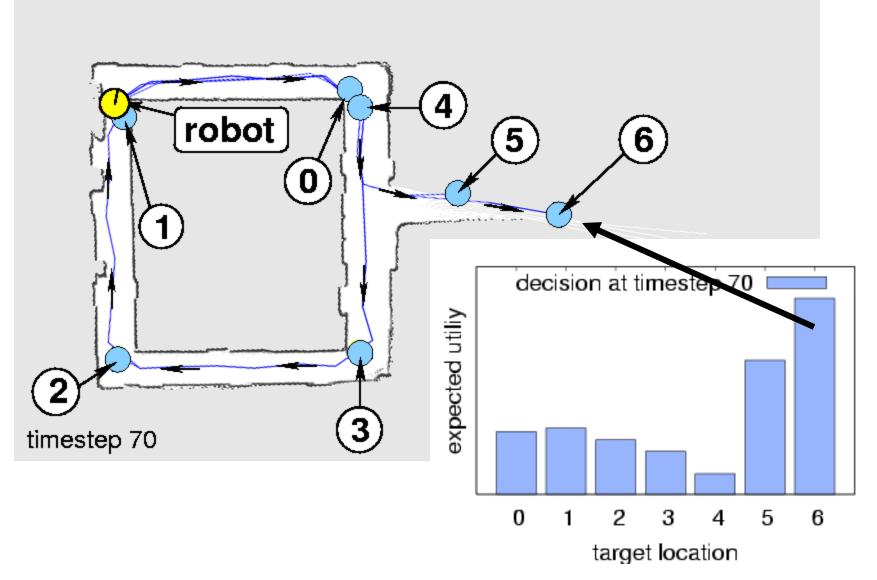
Example: Evaluate Targets



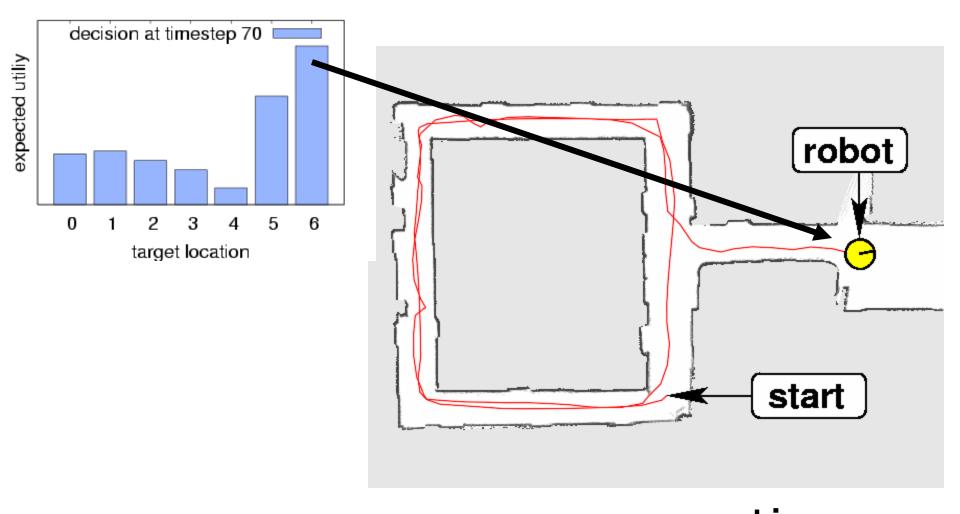
Example: Move Robot to Target



Example: Evaluate Targets

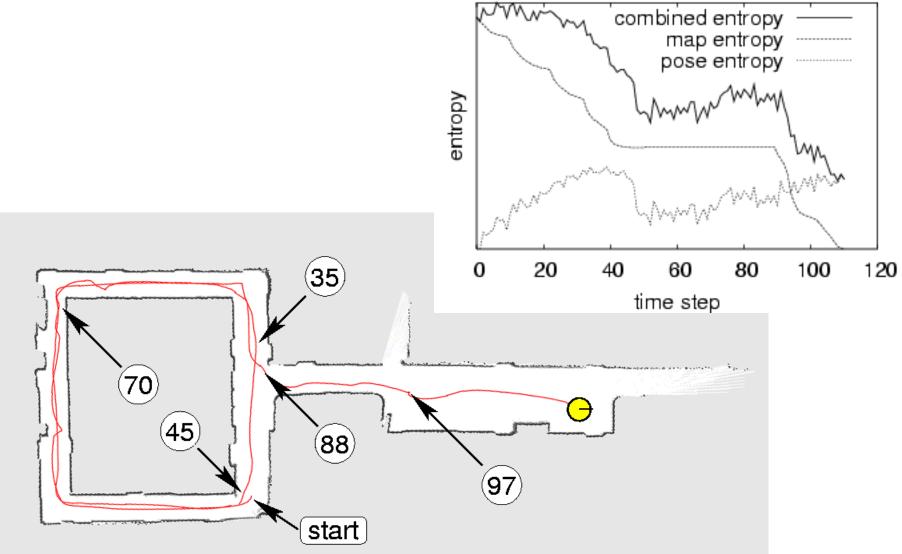


Example: Move Robot



... continue .35

Example: Entropy Evolution



Comparison

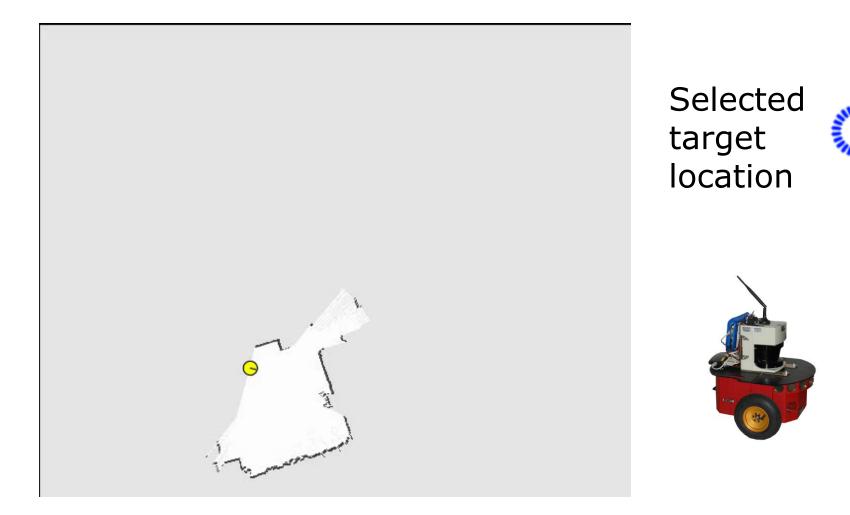
Map uncertainty only:



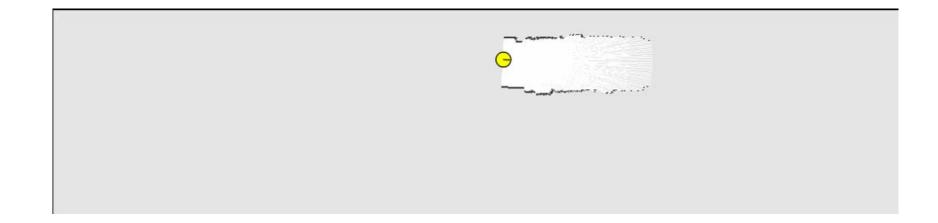
After loop closing action:



Real Exploration Example



Corridor Exploration



- The decision-theoretic approach leads to intuitive behaviors: "re-localize before getting lost"
- Some animals show a similar behavior (dogs marooned in the tundra of north Russia)

Summary

- A decision-theoretic approach to exploration in the context of RBPF-SLAM
- The approach utilizes the factorization of the Rao-Blackwellization to efficiently calculate the expected information gain
- Reasons about measurements obtained along the path of the robot
- Considers a reduced action set consisting of exploration, loop-closing, and placerevisiting actions