### Introduction to Mobile Robotics

### **Wheeled Locomotion**

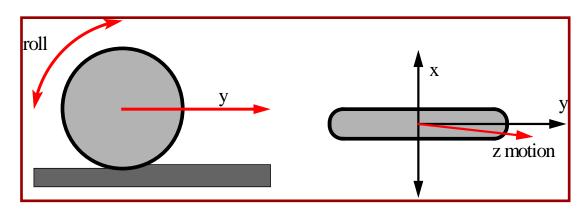
Wolfram Burgard



# **Locomotion of Wheeled Robots**

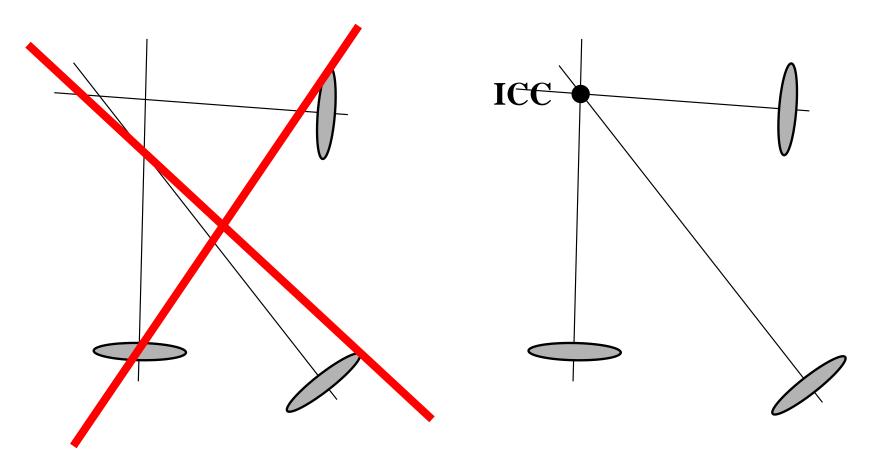
Locomotion (Oxford Dict.): Power of motion from place to place

- Differential drive (AmigoBot, Pioneer 2-DX)
- Car drive (Ackerman steering)
- Synchronous drive (B21)
- XR4000
- Mecanum wheels



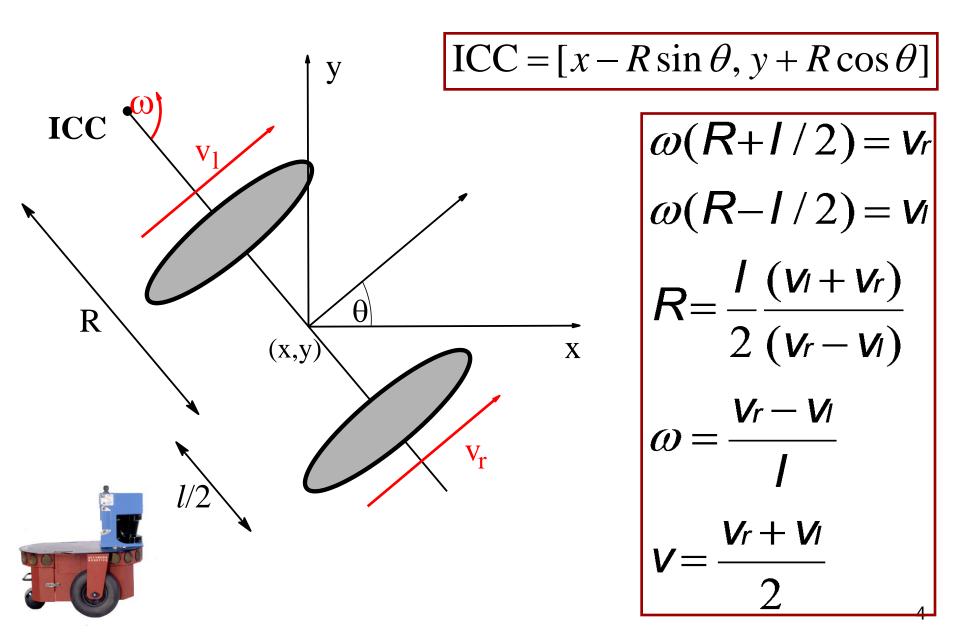
we also allow wheels to rotate around the z axis

### **Instantaneous Center of Curvature**



 For rolling motion to occur, each wheel has to move along its y-axis

### **Differential Drive**



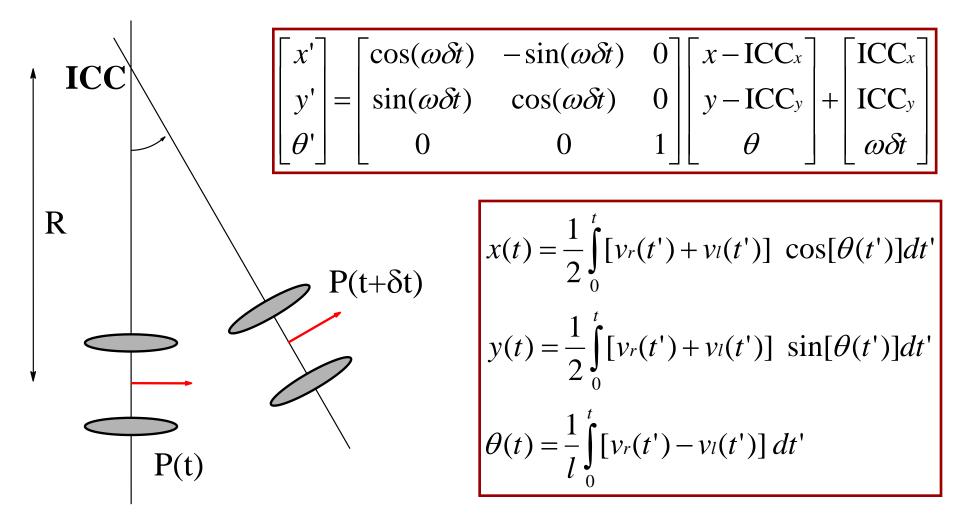
#### **Differential Drive: Forward Kinematics**

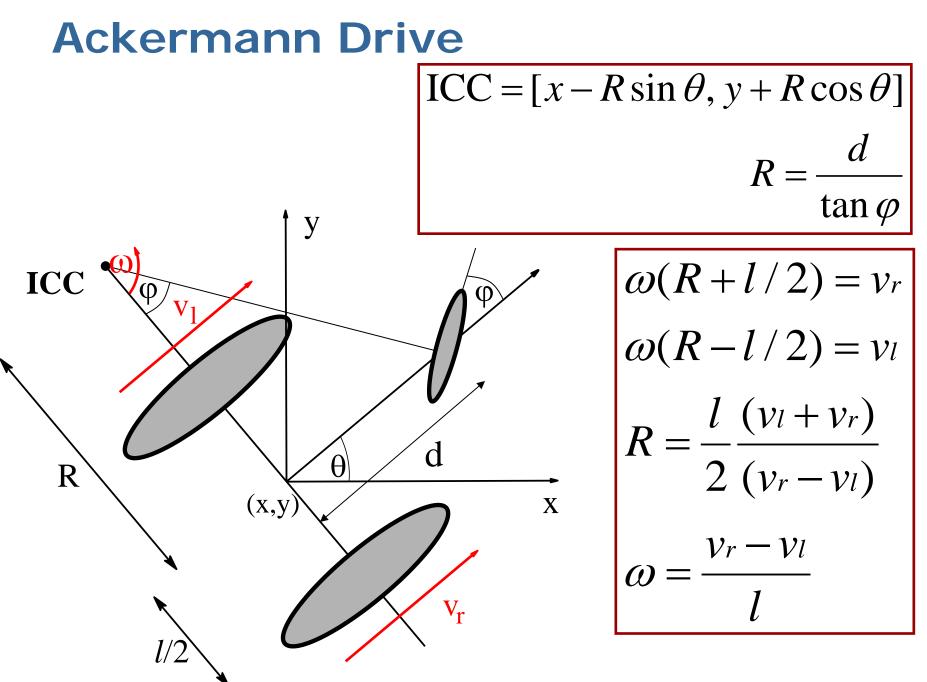
ICC  

$$\begin{bmatrix} x'\\ y'\\ \theta' \end{bmatrix} = \begin{bmatrix} \cos(\omega\delta t) & -\sin(\omega\delta t) & 0\\ \sin(\omega\delta t) & \cos(\omega\delta t) & 0\\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x - ICC_x\\ y - ICC_y\\ \theta \end{bmatrix} + \begin{bmatrix} ICC_x\\ ICC_y\\ \omega\delta t \end{bmatrix}$$
R  

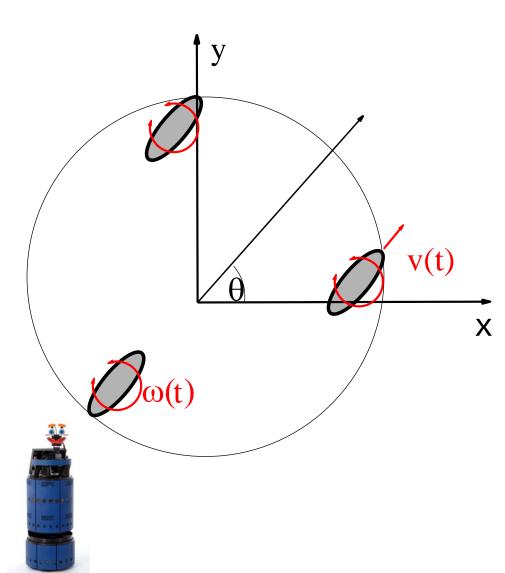
$$\begin{aligned} R \\ P(t+\delta t) \\ P(t+\delta t) \\ P(t) \end{bmatrix} x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt' \\ y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt' \\ \theta(t) = \int_{0}^{t} \omega(t') dt' \end{aligned}$$

#### **Differential Drive: Forward Kinematics**



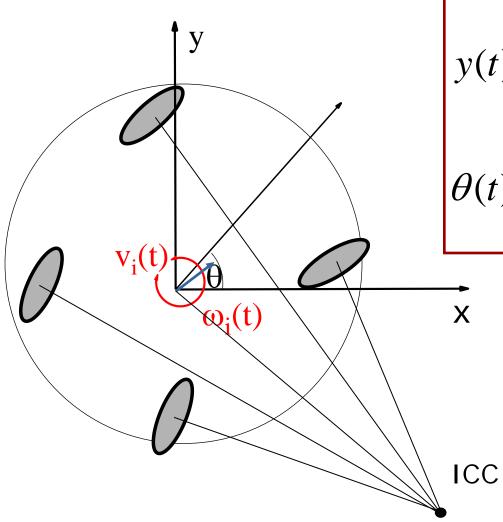


### **Synchronous Drive**



$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$
$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$
$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$





$$x(t) = \int_{0}^{t} v(t') \cos[\theta(t')]dt'$$
$$y(t) = \int_{0}^{t} v(t') \sin[\theta(t')]dt'$$
$$\theta(t) = \int_{0}^{t} \omega(t') dt'$$



#### Mecanum Wheels



$$v_{y} = (v_{0} + v_{1} + v_{2} + v_{3})/4$$
  

$$v_{x} = (v_{0} - v_{1} + v_{2} - v_{3})/4$$
  

$$v_{\theta} = (v_{0} + v_{1} - v_{2} - v_{3})/4$$
  

$$v_{error} = (v_{0} - v_{1} - v_{2} + v_{3})/4$$

### The Kuka OmniRob Platform



### Example: KUKA youBot



### **Tracked Vehicles**









### **Other Robots: OmniTread**



[courtesy by Johann Borenstein]

### **Non-Holonomic Constraints**

- Non-holonomic constraints limit the possible incremental movements within the configuration space of the robot.
- Robots with differential drive or synchrodrive move on a circular trajectory and cannot move sideways.
- Mecanum-wheeled robots can move sideways (they have no non-holonomic constraints).

# Holonomic vs. Non-Holonomic

- Non-holonomic constraints reduce the control space with respect to the current configuration
  - E.g., moving sideways is impossible.
- Holonomic constraints reduce the configuration space.
  - E.g., a train on tracks (not all positions and orientations are possible)

# Drives with Non-Holonomic Constraints

- Synchro-drive
- Differential drive
- Ackermann drive





# Drives without Non-Holonomic Constraints

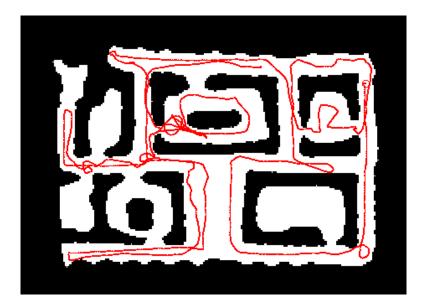
Mecanum wheels

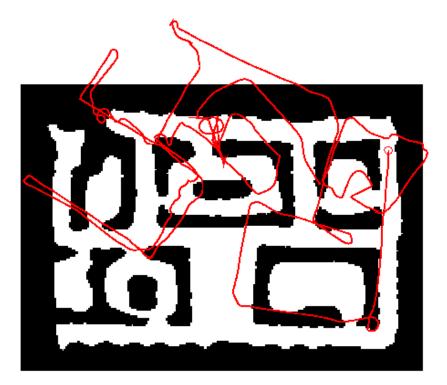




# **Dead Reckoning and Odometry**

- Estimating the motion based on the issued controls/wheel encoder readings
- Integrated over time





## Summary

- Introduced different types of drives for wheeled robots
- Math to describe the motion of the basic drives given the speed of the wheels
- Non-holonomic constraints
- Odometry and dead reckoning