



$$R_1 \dots R_n B = R'_1 \dots R'_n \quad ; \quad R_k \text{ relative rotations}$$

\$\Rightarrow\$ Goal: Find \$R'\_1 \dots R'\_n\$

\* let the first node be the Ref. frame

\* we want one rotation axis for the correction

$$\Rightarrow \begin{matrix} A'_n \\ \text{"} \\ R'_{1:n} \end{matrix} = \begin{matrix} A_n B \\ \text{"} \\ R_{1:n} \end{matrix} = Q A_n \quad \text{with } A_n \text{ being the rotation in the global frame}$$

$$Q := Q_1 \dots Q_n$$

$$Q_k = \text{sterp}(Q, u_{k-1})^T \text{sterp}(Q, u_k) \quad u_k \in [0, 1]$$

$$R'_k = [A'_{k-1}]^T A'_k \quad \leftarrow \quad A'_k = Q_1 \dots Q_k A_k$$

$$= [Q_{1:k-1} A_{k-1}]^T A'_k$$

$$= A_{k-1}^T Q_{k-1}^T \dots Q_1^T A'_k$$

$$= A_{k-1}^T Q_{k-1} \dots Q_1^T [Q_1 \dots Q_k A_k]$$

$$= A_{k-1}^T Q_k A_k$$

$$= (R_{1:k-1})^T Q_k R_{1:k}$$