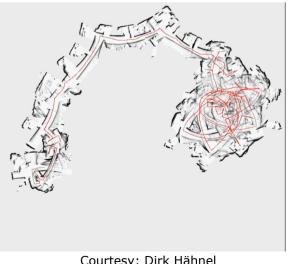


Mapping With Raw Odometry



Motivation

- So far, we addressed landmark-based SLAM (EKF, SEIF, FastSLAM)
- We learned how to build grid maps assuming "known poses"

Today: SLAM for building grid maps

Observation

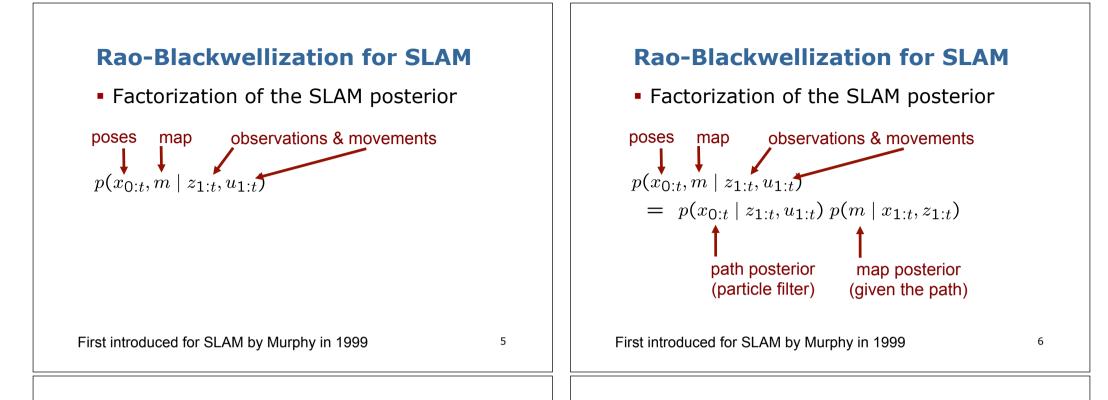
• Assuming known poses fails!

Questions

- Can we solve the SLAM problem if no pre-defined landmarks are available?
- Can we use the ideas of FastSLAM to build grid maps?

Courtesy: Dirk Hähnel

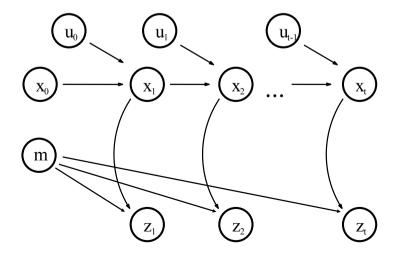
4



Grid-based SLAM

- As with landmarks, the map depends on the poses of the robot during data acquisition
- If the poses are known, grid-based mapping is easy ("mapping with known poses")

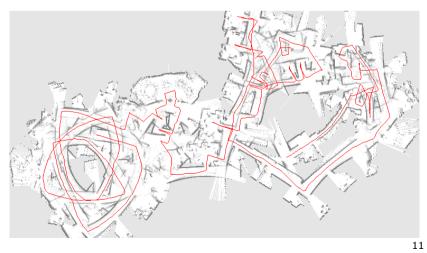
A Graphical Model for Grid-Based SLAM



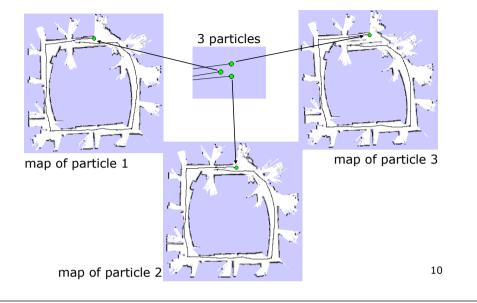
Grid-Based Mapping with Rao-Blackwellized Particle Filters

- Each particle represents a possible trajectory of the robot
- Each particle maintains its own map
- Each particle updates it using "mapping with known poses"

Performance of Grid-based FastSLAM 1.0



Particle Filter Example



Problem

- Too many samples are needed to sufficiently model the motion noise
- Increasing the number of samples is difficult as each map is quite large
- Idea: Improve the proposal to generate a better prediction. This reduces the required number of particles

Improved Proposal

 Compute an improved proposal that considers the most recent observation

 $x_t^{[k]} \sim p(x_t \mid x_{1:t-1}^{[k]}, u_{1:t}, z_{1:t})$

Goals:

- More precise sampling
- More accurate maps
- Less particles needed

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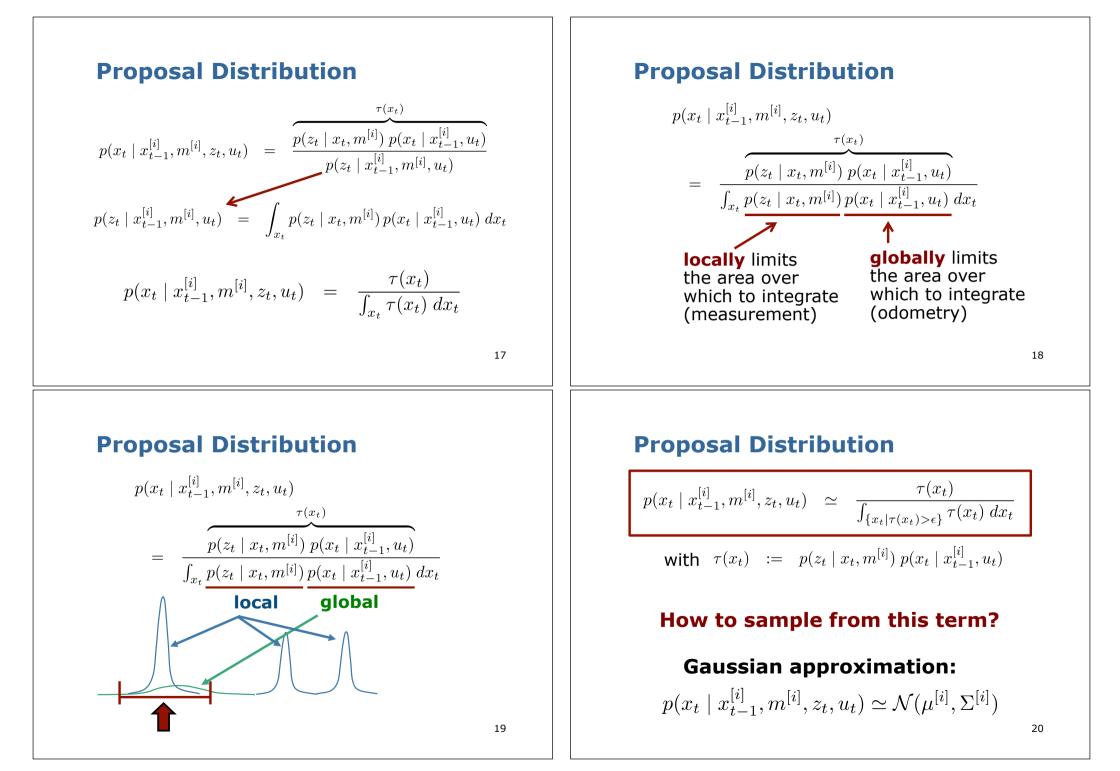
Proposal Distribution

$$p(x_{t} | x_{t-1}^{[i]}, m^{[i]}, z_{t}, u_{t}) = \frac{\overbrace{p(z_{t} | x_{t}, m^{[i]}) \ p(x_{t} | x_{t-1}^{[i]}, u_{t})}^{\tau(x_{t})}}{p(z_{t} | x_{t-1}^{[i]}, m^{[i]}, u_{t})}$$
15

The Optimal Proposal Distribution [Arulampalam et al., 01] $p(x_t \mid x_{t-1}^{[i]}, m^{[i]}, z_t, u_t) = \frac{p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t)}{p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t)}$ For lasers $p(z_t | x_t, m^{[i]})$ is typically peaked and dominates the product 14 **Proposal Distribution**

$$p(x_t \mid x_{t-1}^{[i]}, m^{[i]}, z_t, u_t) = \frac{p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t)}{p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t)}$$

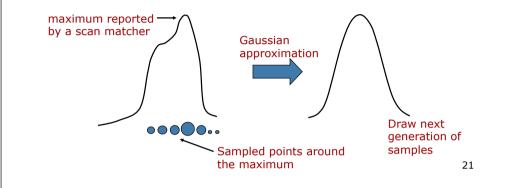
$$p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t) = \int_{x_t} p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t) dx_t$$



Gaussian Proposal Distribution

 $p(x_t \mid x_{t-1}^{[i]}, m^{[i]}, z_t, u_t) \simeq \frac{\tau(x_t)}{\int_{\{x_t \mid \tau(x_t) > \epsilon\}} \tau(x_t) \, dx_t}$

Approximate this equation by a Gaussian:



Computing the Importance Weight

$$w_t^{[i]} = w_{t-1}^{[i]} p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t)$$

[Arulampalam et al., 01]

Estimating the Parameters of the Gaussian for Each Particle

$$\mu^{[i]} = \frac{1}{\eta} \sum_{j=1}^{K} x_j \tau(x_j)$$

$$\Sigma^{[i]} = \frac{1}{\eta} \sum_{j=1}^{K} (x_j - \mu^{[i]}) (x_j - \mu^{[i]})^T \tau(x_j)$$

 x_j are points sampled around the location x^* to which the scan matching has converged to

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Computing the Importance Weight

$$w_t^{[i]} = w_{t-1}^{[i]} p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t) = w_{t-1}^{[i]} \int_{x_t} p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t) dx_t$$

Computing the Importance Weight

$$w_t^{[i]} = w_{t-1}^{[i]} p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t)$$

= $w_{t-1}^{[i]} \int_{x_t} \underbrace{p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t)}_{\tau(x_t)} dx_t$

25

Computing the Importance Weight

Computing the Importance Weight

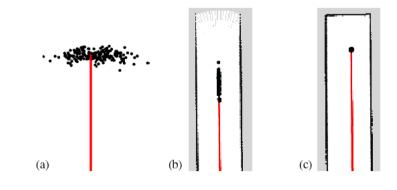
$$w_t^{[i]} = w_{t-1}^{[i]} p(z_t \mid x_{t-1}^{[i]}, m^{[i]}, u_t)$$

= $w_{t-1}^{[i]} \int_{x_t} p(z_t \mid x_t, m^{[i]}) p(x_t \mid x_{t-1}^{[i]}, u_t) dx_t$
 $\simeq w_{t-1}^{[i]} \int_{\{x_t \mid \tau(x_t) > \epsilon\}} \tau(x_t) dx_t$

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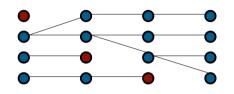
Improved Proposal

 The proposal adapts to the structure of the environment



Resampling

- Resampling at each step limits the "memory" of our filter
- Suppose we loose each time 25% of the particles, this may lead to:



• Goal: Reduce the resampling actions

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Number of Effective Particles

 Empirical measure of how well the target distribution is approximated by samples drawn from the proposal

$$n_{eff} = \sum_{i} \left(w_t^{[i]} \right)^{-2}$$

- *n_{eff}* describes "the inverse variance of the **normalized** particle weights"
- For equal weights, the sample approximation is close to the target

Selective Resampling

- Resampling is necessary to achieve convergence
- Resampling is dangerous, since important samples might get lost ("particle depletion")
- Resampling makes only sense if particle weights differ significantly

• Key question: When to resample?

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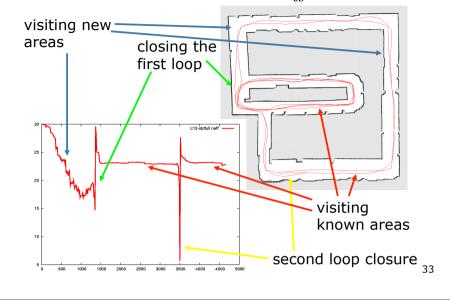
Resampling with n_{eff}

- If our approximation is close to the target, no resampling is needed
- We only resample when $n_{e\!f\!f}$ drops below a given threshold ($N\!/2$)

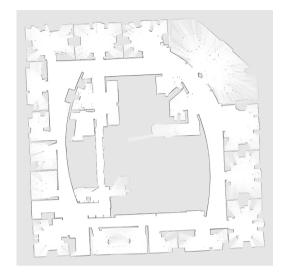
$$\sum_{i} \left(w_t^{[i]}
ight)^{-2} \stackrel{?}{<} N/2$$

• Note: weights need to be normalized [Doucet, '98; Arulampalam, '01]

Typical Evolution of n_{eff}



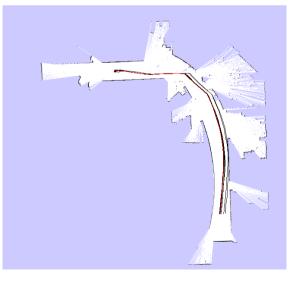
Intel Lab



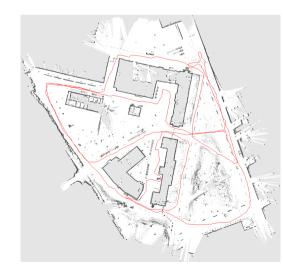
15 particles

- four times faster than real-time P4, 2.8GHz
- 5cm resolution during scan matching
- 1cm resolution in final map

Intel Lab



Outdoor Campus Map



30 particles

- 250x250m²
- 1.75 km (odometry)
- 30cm resolution in final map

MIT Killian Court



• The "infinite-corridor-dataset" at MIT

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MIT Killian Court – Video

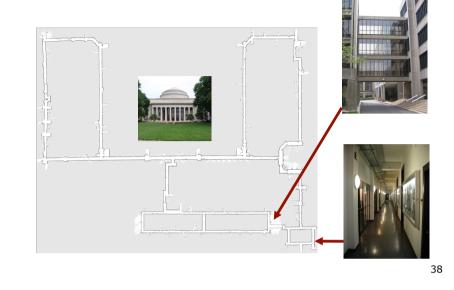


Real World Application

• This guy uses a similar technique...

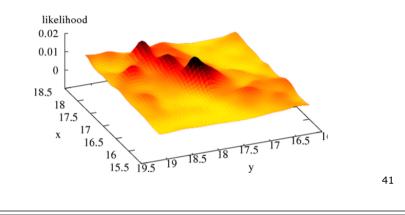


MIT Killian Court



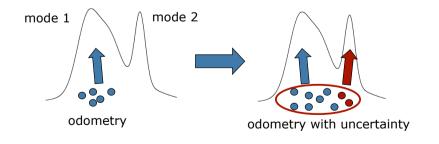
Problems of Gaussian Proposals

- Gaussians are uni-model distributions
- In case of loop-closures, the likelihood function might be multi-modal



Efficient Multi-Modal Sampling

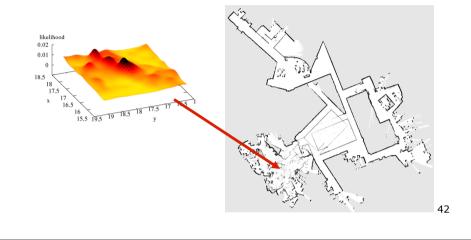
• Approximate the likelihood in a better way!



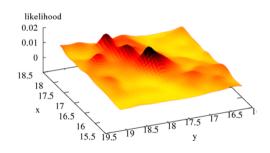
 Sample from odometry first and the use this as the start point for scan matching

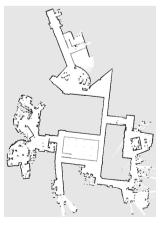
Problems of Gaussian Proposals

 Multi-modal likelihood function can cause filter divergence



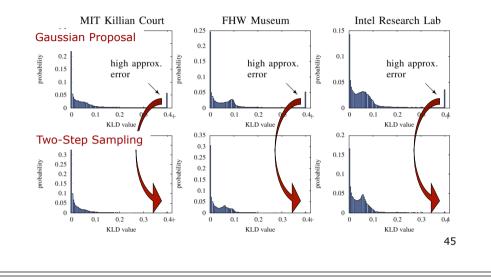
The Two-Step Sampling Works!





...with nearly zero overhead

Difference Between the Optimal Proposal and the Approximations



Gaussian Proposal: Yes or No?

- Gaussian allow for efficient sampling
- Problematic in multi-model cases
- Laser-baser SLAM: 3-6% multi-modal distribution (for the datasets here)
- Gaussian proposals can lead to divergence
- Two-step sampling process overcomes this problem effectively and efficiently

Is a Gaussian an Accurate Choice for the Proposal?

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Conclusion

- The ideas of FastSLAM can also be applied in the context of grid maps
- Improved proposals are essential
- Similar to scan-matching on a perparticle base
- Selective resamples reduces the risk of particle depletion
- Substantial reduction of the required number of particles

Literature

Grid-FastSLAM with Improved Proposals

- Grisetti, Stachniss, Burgard: Improved Techniques for Grid Mapping with Rao-Blackwellized Particle Filters, 2007
- Stachniss, Grisetti, Burgard, Roy. Analyzing Gaussian Proposal Distributions for Mapping with Rao-Blackwellized Particle Filters, 2007

GMapping

- Efficient open source implementation of the presented method (2005-2008)
- C++ Code available via svn co https://svn.openslam.org/data/svn/gmapping

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